

***Waste Form Degradation
Model Status Report: ANL
Mixed Potential Model,
Version 1. Archive***

**Used Fuel Disposition –
Engineered Barrier Systems**

***Prepared for
U.S. Department of Energy
Used Fuel Disposition Campaign***

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SUMMARY

This work is being performed as part of the DOE NE Used Fuel Disposition (UFD) Campaign's Engineered Barrier Systems (EBS) Evaluations, work package: FT-12AN080601. This document represents the December, 2012 milestone report: M3FT-13AN0806013.

The purpose of this work is to develop and optimize a predictive model for the degradation of used uranium oxide fuel that is based on fundamental electrochemical and thermodynamic principals. This process model will provide source terms for radionuclide release the UFD generic performance assessment model. The approach being followed is to implement an existing, well tested electrochemical corrosion model and then extend it to include specific reactions affecting the fuel degradation processes under the disposal scenarios of interest.

This report presents the details of the first version of our UO_2 fuel matrix degradation model. The model described was produced by implementing the Canadian-mixed potential model for UO_2 fuel dissolution (King and Kolar, 1999, King and Kolar, 2003, Shoesmith et al., 2003) using the numerical computing environment and programming language MATLAB (release R2012a on 64-bit platform). The intent of the initial version was to reproduce the approach used by King and Kolar, 1999 to gain experience with the model, identify key model parameters to be measured experimentally or determined from evaluation of the literature, and provide a touchstone for future modifications of the code.

The initial version of the MATLAB implementation of mixed potential model, referred to as the ANL-MPM Version 1, was verified by reproducing published results from the Canadian-MPM reports (Jerden et al., 2012). This report provides a detailed discussion of the actual coding that was used in the implementation of ANL-MPM Version 1.

The ANL-MPM Version 1 (MATLAB implementation of the Canadian-MPM described by King and Kolar, 1999) is a 1-dimensional reaction-diffusion model that accounts for the following processes:

- Interfacial redox reaction kinetics influencing oxidative dissolution of the UO_2 matrix.
- Chemical or solubility based dissolution of the fuel matrix.
- Complexation of dissolved uranium by carbonate near the fuel surface and in the bulk solution.
- Production of hydrogen peroxide (which is the dominant fuel oxidant in anoxic repository environments) by alpha-radiolysis.
- Diffusion of reactants and products in the groundwater away from and towards the reacting fuel surface.
- Precipitation and dissolution of a U-bearing corrosion product layer on the fuel surface.
- Adsorption of uranium onto iron oxides.
- Arrhenius-type temperature dependence for all interfacial and bulk reactions.

The ANL-MPM Version 1 will be used as a base-line check for future versions of the ANL-MPM. A working beta version of the ANL-MPM Version 2 has been implemented and is now

being tested and optimized. The ANL-MPM Version 2 accounts for the following processes and conditions (in addition to processes listed above):

- Quantifies the oxidation of dissolved H_2 at the used fuel/solution interface: H_2 concentration to be supplied by other EBS model or user specified).
- Represents the NMPs as a separate domain at the used fuel/solution interface. The "size" of the NMP domain (relative to the fuel) is specified by the user in terms of a surface coverage and is electrically linked with the UO_2 matrix by a user adjustable resistance. This will allow the effects of NMP corrosion and sorption on the catalytic efficiency to be taken into account.
- Quantifies the bulk decomposition of hydrogen peroxide (with temperature dependence).
- Provides option for user to specify temperature and dose profiles of the fuel (profiles can be constant single values or functions).
- Includes Rapid diffusion option to facilitate the calculation of concentrations of species whose diffusion coefficients are sufficiently large that they reach steady state on the order of days (decreases computer time needed for model convergence).

This report focuses on the base-line model ANL-MPM Version 1; for a discussion of the conceptual basis for the ANL-MPM Version 2 see Jerden et al., 2012.

Because the ANL-MPM is based on fundamental principles, it is flexible enough to be applied to the full range of repository environments as well as shorter-term storage scenarios being considered as part of the UFD campaign. On-going experimental work described in Jerden et al., 2012 and Ebert et al., 2012 is focused on providing key model parameter values that are needed to improve predictive accuracy and capabilities of the ANL-MPM.

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ACRONYMS

ANL	Argonne National Laboratory
DOE NE	Department of Energy Nuclear Energy
EBS	Engineered Barrier System
GPAM	Generic Performance Assessment Model
GSPM	Generic System Performance Model
MPM	Mixed Potential Model
NMP	Noble Metal bearing Particle
UFD	Used Fuel Disposition

ANL Mixed Potential Model Version 1 Archive

1. INTRODUCTION AND BACKGROUND

This work was performed as part of the DOE NE Used Fuel Disposition (UFD) Campaign's Engineered Barrier Systems (EBS) Evaluations, work package: FT-13AN080601. This document represents the December 20, 2012 milestone report: M3FT-13AN0806013.

1.1. Objectives and Scope

The main purpose of this work is to develop and optimize a predictive model for the degradation of used uranium oxide fuel that is based on fundamental electrochemical and thermodynamic principals. This process model will be integrated with the UFD generic performance assessment model to provide a source term for radionuclide release for a disposal scenario of interest. The approach has been to implement, optimize and extend an existing, well tested electrochemical corrosion model to specific fuel degradation processes and mechanisms of interest. The conceptual context for our modeling work within the larger UFD research campaign is shown in Figure 1.

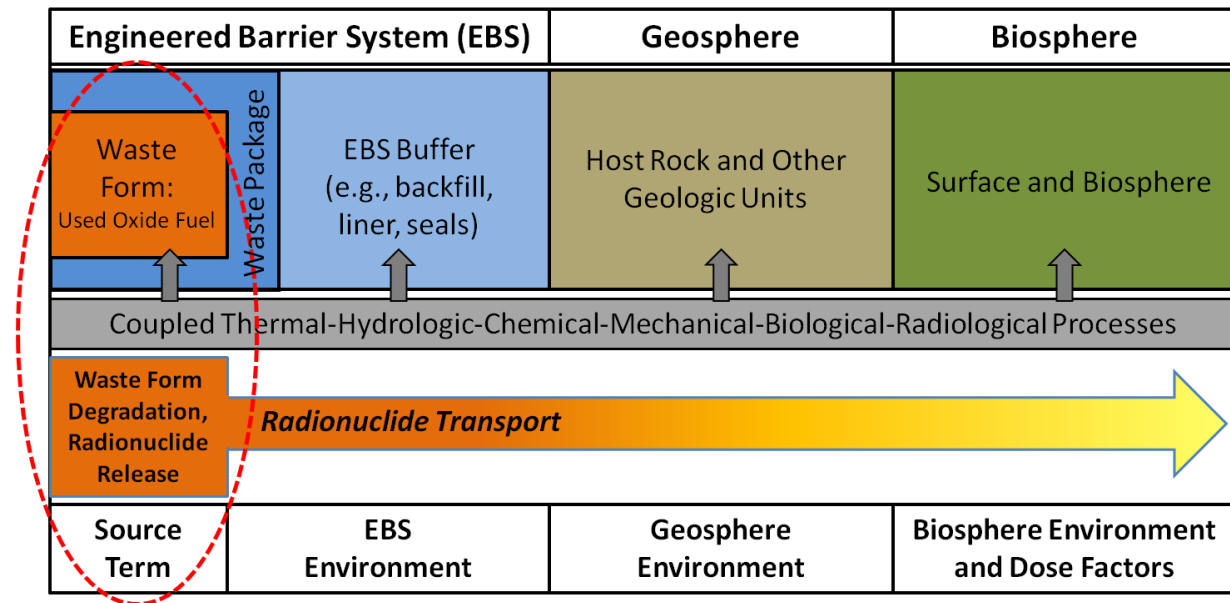


Figure 1. Components of a generic disposal system for used oxide fuel (adapted from Freeze et al. 2010). The red circle identifies the components and associated processes targeted by the experiments described in this report.

This report presents the details of the first version of our UO₂ fuel matrix degradation model. The model described was produced by implementing the Canadian-mixed potential model for UO₂ fuel dissolution (King and Kolar, 1999, King and Kolar, 2003, Shoesmith et al., 2003) using the numerical computing environment and programming language MATLAB. MATLAB release R2012a, for a 64-bit platform was used to implement the ANL-MPM Version 1.

This work has provided a working, base-line model that is being modified and extended to include additional reactions and factors affecting fuel dissolution. The initial version of the MATLAB implementation of mixed potential model, referred to as the ANL-MPM Version 1, was verified by reproducing published results from the Canadian-MPM reports (Jerden et al., 2012). This report provides a detailed discussion of the actual coding that was used in the implementation of ANL-MPM Version 1. This report thus documents the base-line modeling approach (ANL-MPM) on which future versions will be based.

The ANL-MPM Version 1 (MATLAB implementation of the Canadian-MPM described by King and Kolar, 1999) is a 1-dimensional reaction-diffusion model that accounts for the following processes:

- Interfacial redox reaction kinetics influencing oxidative dissolution of the UO_2 matrix.
- Chemical or solubility based dissolution of the fuel matrix.
- Complexation of dissolved uranium by carbonate near the fuel surface and in the bulk solution.
- Production of hydrogen peroxide (which is the dominant fuel oxidant in anoxic repository environments) by alpha-radiolysis.
- Diffusion of reactants and products in the groundwater away from and towards the reacting fuel surface.
- Precipitation and dissolution of a U-bearing corrosion product layer on the fuel surface.
- Adsorption of uranium onto iron oxides.
- Arrhenius-type temperature dependence for all interfacial and bulk reactions.

Our modeling approach was divided into two stages: (1) implementation of the Canadian-MPM in the programming language MATLAB with only minor changes to the original model. The scripts resulting from this work are referred to as the ANL-MPM Version 1 and are the focus of this report. (2) Extension and optimization of the MPM implemented in MATLAB. This model, which is still under development, is referred to as the ANL-MPM Version 2. The Version 2 of the ANL-MPM quantifies the effects of dissolved hydrogen and the catalytic properties of NMP on fuel matrix dissolution. It has been optimized from a computing standpoint (relative to V1) by using a rapid diffusion approach which significantly decreases the time it takes for the model to converge on a unique solution and facilitates calculations of long-term behavior.

Sensitivity studies of the ANL-MPM Version 1 (presented in Jerden et al., 2012) have been used to identify key model parameters for which values must be determined from literature data, measured experimentally, or calculated with submodels, such as the concentrations of radiolytic products, for application to conditions other than those used in the Canadian-MPM. The focus of our model sensitivity studies and linked experimental work is on demonstrating and improving the applicability of the ANL-MPM to the full range of generic repository concepts being considered as part of the UFD campaign.

Because the ANL-MPM is based on fundamental principles, it is flexible enough to be applied to the full range of repository environments as well as shorter-term storage scenarios being considered as part of the UFD campaign. On-going experimental work described in Jerden et al.,

2012 and Ebert et al., 2012 is focused on providing key model parameter values that are needed to improve predictive accuracy and capabilities of the ANL-MPM.

2. ANL-MPM V1: CONCEPTUAL AND MATHEMATICAL BASIS

2.1. Model Assumptions, Mass-balance Equations and Reactions

The Canadian-MPM, on which the ANL-MPM is based, was developed to predict the corrosion behavior of used fuel inside a failed steel container under anticipated conditions in a granitic repository setting (King and Kolar, 1999, King and Kolar, 2003, Shoesmith et.al., 2003). Since the model is based on fundamental electrochemical and thermodynamic principals it is flexible in its application and can be extended to other repository environments of interest (a focus of ongoing work as part of ANL's UFD research). Figure 2 shows the conceptual set-up for both the ANL-MPM Version 1 and the Canadian-MPM on which it is based.

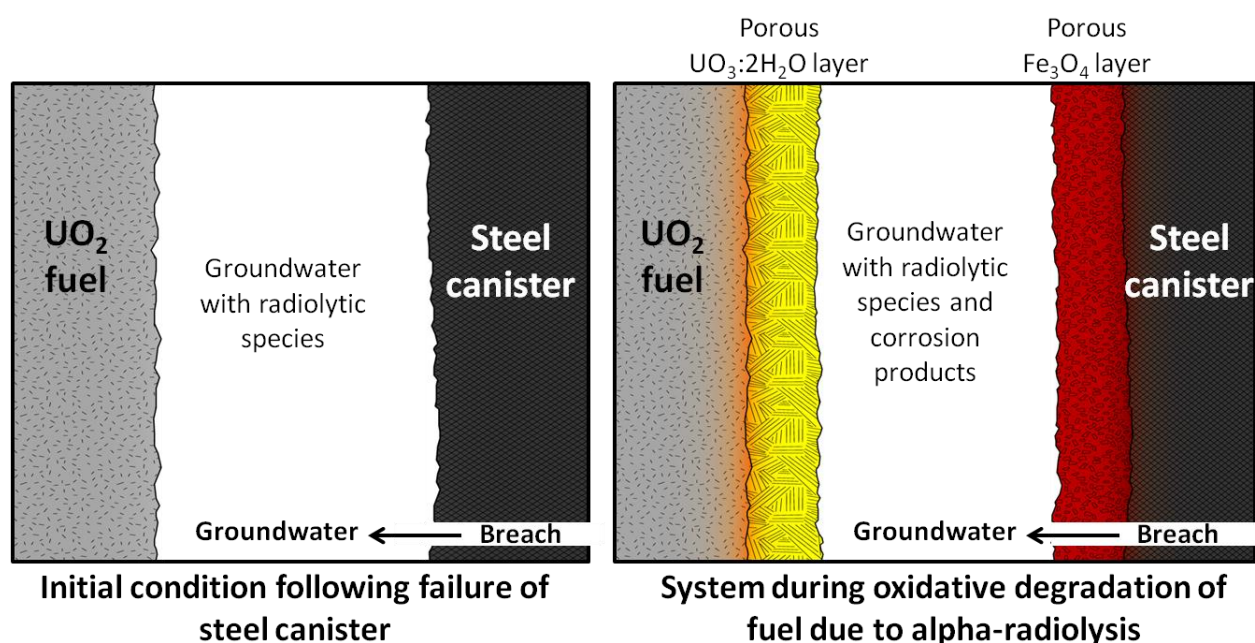


Figure 2. Simplified representation of breached canister system used in the Canadian-MPM (King and Kolar, 1999, King and Kolar, 2003, Shoesmith et.al., 2003) on which the ANL-MPM Version 1 (topic of this report) is based. This is a process model for the oxidative degradation of UO_2 fuel due to alpha radiolysis of groundwater.

The Canadian-MPM and ANL-MPM Version 1 both consist of ten one-dimensional reaction-diffusion equations (Equations 1 - 10), each describing the mass transport, precipitation/dissolution, adsorption/desorption and redox processes of the ten chemical species included in the model. Electrochemical rate expressions are used as boundary conditions for species that participate in the interfacial electrochemical reactions (King and Kolar, 1999, King and Kolar, 2003, Shoesmith et.al., 2003).

Table 1 identifies the chemical species (components) involved in Equations 1 - 10. These mass-balance equations are solved over a non-uniform spatial grid that is bounded by a UO₂ fuel surface on one side and steel surface (representing canister material) on the other. For a given set of conditions these bounding surface undergo oxidative-dissolution and thus represent sources of dissolved uranium and iron in the model.

The reactions that feed into Equations 1 - 10 are written out in Table 2 and shown in a two dimensional representation of the ANL-MPM Version 1 in Figure 4. Reaction-diffusion mass-balance equations on which the Canadian and ANL mixed potential models are based (see Table 1 for symbol identification):

$$\begin{aligned} \varepsilon \frac{\partial C_{\text{UO}_2^{2+}}}{\partial t} = \frac{\partial}{\partial x} \left(\tau_f \varepsilon D_{\text{UO}_2^{2+}} \frac{\partial C_{\text{UO}_2^{2+}}}{\partial x} \right) - \varepsilon k_8 C_{\text{UO}_2^{2+}} (C_{\text{U(VI)ads}}^{\text{max}} - C_{\text{U(VI)ads}}) \rho \\ + k_{-8} C_{\text{U(VI)ads}} \rho - \varepsilon k_5 C_{\text{UO}_2^{2+}} C_{\text{Fe}^{2+}} - \varepsilon k_1 \max(0, C_{\text{UO}_2^{2+}} - C_{\text{UO}_2^{2+}}^{\text{sat}}) \end{aligned} \quad (\text{Eq.1})$$

$$\begin{aligned} \varepsilon \frac{\partial C_{\text{UO}_2(\text{CO}_3)_2}}{\partial t} = \frac{\partial}{\partial x} \left(\tau_f \varepsilon D_{\text{UO}_2(\text{CO}_3)_2} \frac{\partial C_{\text{UO}_2(\text{CO}_3)_2}}{\partial x} \right) \\ - \varepsilon k_9 C_{\text{UO}_2(\text{CO}_3)_2} (C_{\text{U(VI)ads}}^{\text{max}} - C_{\text{U(VI)ads}}) \rho + k_{-9} C_{\text{U(VI)ads}} \rho - \varepsilon k_6 C_{\text{UO}_2(\text{CO}_3)_2} C_{\text{Fe}^{2+}} \\ - \varepsilon k_2 \max(0, C_{\text{UO}_2(\text{CO}_3)_2} - C_{\text{UO}_2(\text{CO}_3)_2}^{\text{sat}}) + k_{-2} C_{\text{CO}_3^2}^{\text{p}} \delta(x-x_A) \end{aligned} \quad (\text{Eq.2})$$

$$\begin{aligned} \varepsilon \frac{\partial C_{\text{U(VI)ads}}}{\partial t} = \varepsilon k_8 C_{\text{UO}_2^{2+}} (C_{\text{U(VI)ads}}^{\text{max}} - C_{\text{U(VI)ads}}) \rho - k_{-8} C_{\text{U(VI)ads}} \rho \\ + \varepsilon k_9 C_{\text{UO}_2(\text{CO}_3)_2} (C_{\text{U(VI)ads}}^{\text{max}} - C_{\text{U(VI)ads}}) \rho - k_{-9} C_{\text{U(VI)ads}} \rho \end{aligned} \quad (\text{Eq.3})$$

$$\varepsilon \frac{\partial C_{\text{(IV)reprecip}}}{\partial t} = \varepsilon k_5 C_{\text{UO}_2^{2+}} C_{\text{Fe}^{2+}} + \varepsilon k_6 C_{\text{UO}_2(\text{CO}_3)_2} C_{\text{Fe}^{2+}} \quad (\text{Eq.4})$$

$$\begin{aligned} \varepsilon \frac{\partial C_{\text{CO}_3^2}}{\partial t} = \frac{\partial}{\partial x} \left(\tau_f \varepsilon D_{\text{CO}_3^2} \frac{\partial C_{\text{CO}_3^2}}{\partial x} \right) + \varepsilon k_9 C_{\text{UO}_2(\text{CO}_3)_2} (C_{\text{U(VI)ads}}^{\text{max}} - C_{\text{U(VI)ads}}) \rho - \\ 2k_{-9} C_{\text{U(VI)ads}} \rho + 2\varepsilon k_6 C_{\text{UO}_2^{2+}} C_{\text{Fe}^{2+}} + 2\varepsilon k_2 \\ \max(0, C_{\text{UO}_2(\text{CO}_3)_2} - C_{\text{UO}_2(\text{CO}_3)_2}^{\text{sat}}) - 2k_{-2} \delta(x-x_A) \end{aligned} \quad (\text{Eq.5})$$

$$\varepsilon \frac{\partial C_{\text{O}_2}}{\partial t} = \frac{\partial}{\partial x} \left(\tau_f \varepsilon D_{\text{O}_2} \frac{\partial C_{\text{O}_2}}{\partial x} \right) - \varepsilon k_3 C_{\text{O}_2} C_{\text{Fe}^{2+}} \quad (\text{Eq.6})$$

$$\varepsilon \frac{\partial C_{H_2O_2}}{\partial t} = \frac{\partial}{\partial x} \left(\tau_f \varepsilon D_{H_2O_2} \frac{\partial C_{H_2O_2}}{\partial x} \right) + \varepsilon G_{H_2O_2} R_D - \varepsilon k_4 C_{H_2O_2} C_{Fe^{2+}} \quad (\text{Eq.7})$$

$$\varepsilon \frac{\partial C_{Fe^{2+}}}{\partial t} = \frac{\partial}{\partial x} \left(\tau_f \varepsilon D_{Fe^{2+}} \frac{\partial C_{Fe^{2+}}}{\partial x} \right) - 4\varepsilon k_3 C_{O_2} C_{Fe^{2+}} - 2\varepsilon k_4 C_{H_2O_2} C_{Fe^{2+}} - 2\varepsilon k_5 C_{UO_2^{2+}} C_{Fe^{2+}} - 2\varepsilon k_6 C_{UO_2CO_3} C_{Fe^{2+}} - \varepsilon k_7 \max(0, C_{Fe^{2+}} - C_{Fe^{2+}}^{sat}) + k_{-7} \delta(x-x_B) \quad (\text{Eq.8})$$

$$\varepsilon \frac{\partial C_A}{\partial t} = \varepsilon k_1 \max(0, C_{UO_2^{2+}} - C_{UO_2^{2+}}^{sat}) + \varepsilon k_2 \max(0, C_{UO_2(CO_3)_2} - C_{UO_2(CO_3)_2}^{sat}) - k_2 C_{CO_3^2}^p \delta(x-x_A) \quad (\text{Eq.9})$$

$$\varepsilon \frac{\partial C_B}{\partial t} = \varepsilon k_7 \max(0, C_{Fe^{2+}} - C_{Fe^{2+}}^{sat}) - k_{-7} \delta(x-x_A) \quad (\text{Eq.10})$$

Table 1. Description of symbols used in The mass-balance Equations 1 - 10. See Appendix 1 for default parameter values used in the ANL-MPM Version 1, MATLAB scripts.

Symbol	Parameter
k_i	Rate of reaction i (see Table 2 and Figure 3)
ε	Total porosity of corrosion layer
τ_f	Tortuosity factor for corrosion layer
ρ	Density of corrosion layer (mole/m ³)
$C_{UO_2^{2+}}$	Dissolved concentration (mole/m ³)
$D_{UO_2^{2+}}$	Bulk-solution diffusion coefficient (m ² /sec)
$C_{UO_2^{2+}}^{sat}$	Saturation concentration (mole/m ³)
$C_{U(VI)ads}$	U(VI) adsorbed to Fe ₃ O ₄ layer (mole/g)
$C_{U(VI)ads}^{max}$	Adsorption capacity of UO ₂ ²⁺ on Fe(II) corrosion layer (mole/g)
$C_{UO_2(CO_3)_2}$	Dissolved concentration (mole/m ³)
$D_{UO_2(CO_3)_2}$	Bulk-solution diffusion coefficient (m ² /sec)
$C_{UO_2(CO_3)_2}^{sat}$	Saturation concentration (mole/m ³)
$C_{(IV)reprecip}$	Concentration of U(IV) formed by reduction of U(VI) by iron (mole/m ³)
$C_{CO_3^2}$	Dissolved concentration (mole/m ³)
$D_{CO_3^2}$	Bulk-solution diffusion coefficient (m ² /sec)
C_{O_2}	Dissolved concentration (mole/m ³)

D_{O_2}	Bulk-solution diffusion coefficient (m ² /sec)
$C_{Fe^{2+}}$	Dissolved concentration (mole/m ³)
$D_{Fe^{2+}}$	Bulk-solution diffusion coefficient (m ² /sec)
$C_{Fe^{2+}}^{sat}$	Saturation concentration (mole/m ³)
$C_{H_2O_2}$	Dissolved concentration (mole/m ³)
$D_{H_2O_2}$	Bulk-solution diffusion coefficient (m ² /sec)
$G_{H_2O_2}$	Primary radiolysis yield of H ₂ O ₂ [mol/(J/kg)/m ³]
R_D	Spatial and time-dependent alpha radiation dose [(J/kg)/sec]
C_A	Auxiliary concentration of solid U(VI) (corrosion layer) (mole/m ³)
x_A	Thickness of U(VI) corrosion layer (m)
C_B	Auxiliary concentration of solid Fe(II) (corrosion layer) (mole/m ³)
x_B	Thickness of Fe(II) corrosion layer (m)
δ	Function for dissolution of porous corrosion layer: approximated by finite width profile

*The reactions that feed into Equations 1 - 10 are shown in Table 2 and Figure 4.

A representation of the non-uniform spatial grid (showing calculation points as lines) over which the reaction-diffusion equations are solved is shown in Figure 3. The actual distance between the bounding surfaces and the number of calculation points used in a simulation can be specified by the user; the default values are 50 mm and 250 points respectively.

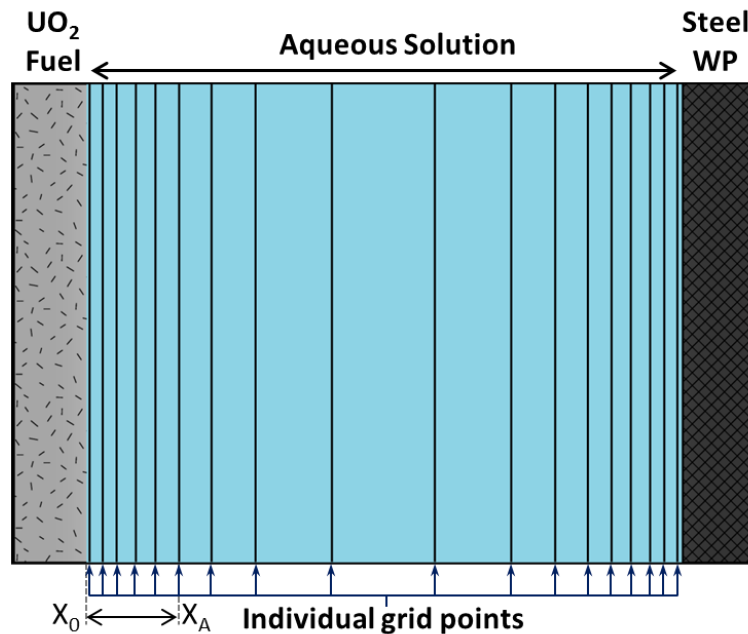
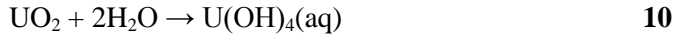


Figure 3. Schematic representation of mixed potential model grid spacing between the used fuel and steel surface boundaries (not all grid intervals are shown). Spacing is logarithmic with finer intervals at the two interfaces. The current implementation of the ANL-MPM

Version 1 contains 250 grid points with a minimum grid spacing of 1 micrometers and a maximum spacing of 1000 micrometers.

Table 2. Surface electrochemical reactions and bulk solution reactions tracked in ANL-MPM Version 1 (symbols map reactions onto Figure 4). For parameter values used to describe each reaction in the MATLAB scripts see Appendices 1 and 2.

Reactions	Symbols for reactions used in Figure 2
<i>Anodic reactions on fuel and steel surfaces</i>	
$\text{UO}_2 \rightarrow \text{UO}_2^{2+} + 2\text{e}^-$	A
$\text{UO}_2 + 2\text{CO}_3^{2-} \rightarrow \text{UO}_2(\text{CO}_3)_2^{2-} + 2\text{e}^-$	B
$\text{H}_2\text{O}_2 \rightarrow \text{O}_2 + 2\text{H}^+ + 2\text{e}^-$	C
$\text{Fe} \rightarrow \text{Fe}^{2+} + 2\text{e}^-$	J
$\text{H}_2 \rightarrow 2\text{H}^+ + 2\text{e}^-$	L*
<i>Cathodic reactions on fuel and steel surfaces</i>	
$\text{H}_2\text{O}_2 + 2\text{e}^- \rightarrow 2\text{OH}^-$	D, H
$\text{O}_2 + 2\text{H}_2\text{O} + 4\text{e}^- \rightarrow 4\text{OH}^-$	E, I
$\text{UO}_2^{2+} + 2\text{e}^- \rightarrow \text{U(IV)}_{\text{reprecipitate}}$	F
$\text{UO}_2(\text{CO}_3)_2^{2-} + 2\text{e}^- \rightarrow \text{U(IV)}_{\text{reprecipitate}} + 2\text{CO}_3^{2-}$	G
$\text{H}_2\text{O} + 4\text{e}^- \rightarrow \frac{1}{2}\text{H}_2(\text{aq}) + \text{OH}^-$	K
<i>Homogeneous Bulk Reactions</i>	
$\text{UO}_2^{2+} + 2\text{H}_2\text{O} \rightarrow \text{UO}_3 \cdot 2\text{H}_2\text{O} + 2\text{H}^+$	1
$\text{UO}_2(\text{CO}_3)_2^{2-} + 2\text{H}_2\text{O} \rightarrow \text{UO}_3 \cdot \text{H}_2\text{O} + 2\text{CO}_3^{2-} + 2\text{H}^+$	2
$\text{UO}_3 \cdot \text{H}_2\text{O} + 2\text{CO}_3^{2-} + 2\text{H}^+ \rightarrow \text{UO}_2(\text{CO}_3)_2^{2-} + 2\text{H}_2\text{O}$	-2
$\text{O}_2 + 2\text{H}_2\text{O} + 4\text{Fe}^{2+} \rightarrow 4\text{Fe(III)} + 4\text{OH}^-$	3
$\text{H}_2\text{O}_2 + 2\text{Fe}^{2+} \rightarrow 2\text{Fe(III)} + 2\text{OH}^-$	4
$\text{UO}_2^{2+} + \text{Fe}^{2+} \rightarrow \text{Fe(III)} + \text{U(IV)}$	5
$\text{UO}_2(\text{CO}_3)_2^{2-} + \text{Fe}^{2+} \rightarrow \text{Fe(III)} + \text{U(IV)} + 2\text{CO}_3^{2-}$	6
$\text{Fe}^{2+} + \text{Fe(III)} + 4\text{H}_2\text{O} \rightarrow \text{Fe}_3\text{O}_4 + 8\text{H}^+$	7
$\text{Fe}_3\text{O}_4 + 8\text{H}^+ \rightarrow \text{Fe}^{2+} + \text{Fe(III)} + 4\text{H}_2\text{O}$	-7
$\text{UO}_2^{2+} \rightarrow (\text{UO}_2^{2+})_{\text{ads}}$	8
$(\text{UO}_2^{2+})_{\text{ads}} \rightarrow \text{UO}_2^{2+}$	-8
$\text{UO}_2(\text{CO}_3)_2^{2-} \rightarrow (\text{UO}_2^{2+})_{\text{ads}} + \text{CO}_3^{2-}$	9
$(\text{UO}_2^{2+})_{\text{ads}} + \text{CO}_3^{2-} \rightarrow \text{UO}_2(\text{CO}_3)_2^{2-}$	-9



*Hydrogen oxidation reaction is not shown in Figure 4 nor in the scripts in Appendix 2. This reaction (L) was not accounted for in the Canadian-MPM of King and Kolar, 1999. It is included conceptually (as a place holder reaction) in anticipation of extending the ANL-MPM to account for how H₂ oxidation at the fuel surface may counter-act oxidative-dissolution processes driven by the formation of radiolytic oxidants (H₂O₂ in model in ANL-MPM Version 1).

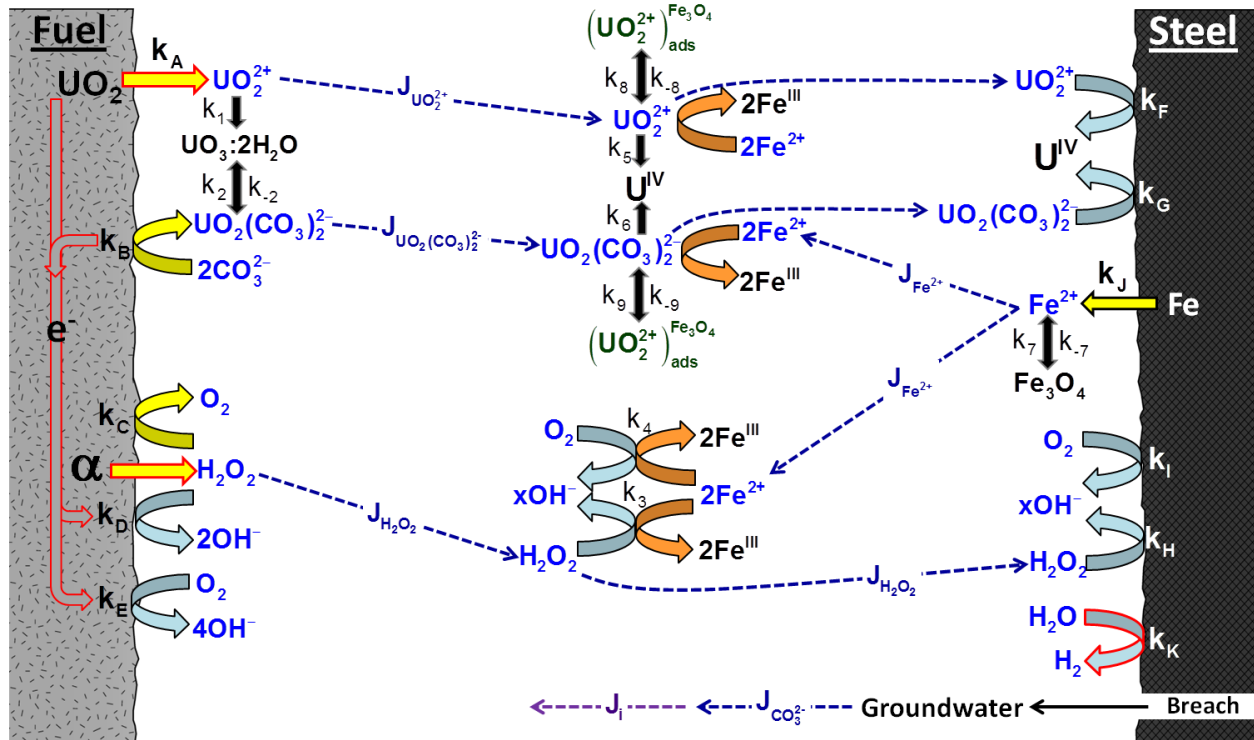


Figure 4. Reaction scheme for ANL-MPM Version 1 and Canadian-MPM of King and Kolar, (1999). Aqueous species are shown in blue, dotted lines represent diffusive fluxes. The “k” labels represent rate expressions for the individual half-reactions. Reactions labeled with letters are for heterogeneous (surface) processes and those labeled with numbers describe homogeneous processes. Anodic reactions are noted with yellow or orange arrows and the cathodic reactions are shown in blue arrows. “ads” stands for adsorbed.

The UO₂ and iron bounding surfaces in the model can host porous layers of corrosion phases that form when the dissolved concentration of U(VI) or Fe(II) reach specified saturation thresholds. These corrosion layers influence the rates of diffusion of species towards and away from the bounding surfaces. The only mode of mass transport in this model is by diffusion (no advection). Other key assumptions retained in the ANL implementation of the Canadian-MPM (in V1 and V2) are:

- 1-D model geometry with non-uniform spatial distribution with emphasis on surface reactions at used fuel and steel (Fe) interfaces.
- Uniform dissolution of fuel surface (no localized effects, e.g., grain boundary etching).

- Mass transport by diffusion only.
- System is saturated with groundwater, the supply of groundwater is not limiting.
- Used fuel cladding is excluded from system.
- U(VI)O₃:2H₂O and Fe₃O₄ corrosion layers are treated as equivalent porous media with spatially and temporally constant porosity and tortuosity.
- U(VI)O₃:2H₂O corrosion layer is assumed to be electrically insulating with electrochemical reactions restricted to areas at base of pores.
- U(VI)O₃:2H₂O corrosion layer attenuates alpha dose rate to solution at the fuel surface.
- U(VI)O₃:2H₂O corrosion layer may contain alpha-emitting radionuclides (user input).
- Fe₃O₄ is assumed to be the stable corrosion product of carbon steel.
- pH is constant (buffered) throughout system.

The non-electrochemical (chemical) dissolution of the UO₂ matrix (Reaction 10, UO₂ + 2H₂O → U(OH)₄(aq), Table 2) is assigned a rate constant of 1x10⁻¹⁷ mole/cm²second (King and Kolar, 1999) and its solubility is modeled using saturation concentration of approximately 1x10⁻⁸ moles/L (King and Kolar, 1999). Due to this low saturation concentration and corresponding slow dissolution rate, the chemical dissolution of the fuel matrix does not represent a significant degradation mechanism in the current model.

2.2. Electrochemical Description of Model Bounding Surfaces (UO₂ and Carbon Steel)

In the ANL-MPM Version 1, the rate of mass loss from the used fuel (a quantification of degradation) is directly related to the corrosion current density by Faradays Law (Equation 11). The corrosion current density is defined as the sum of the current densities of the anodic fuel oxidation reactions (Reactions A and B in Table 2, Equation 12 below).

$$\frac{ML^{Fuel}}{time} = \frac{i_{CORR}^{Fuel} MW^{Fuel}}{nF} \quad (Eq.11)$$

$$i_{CORR}^{Fuel} = i_A + i_B \quad (Eq.12)$$

where $ML^{Fuel}/time$ is the total mass loss rate (grams/m²days) due to oxidative and chemical dissolution, i_{CORR}^{Fuel} is the corrosion current density (amp/m²), MW^{Fuel} is the molecular weight (grams/mole), n is the number of electrons transferred, F is the Faraday constant C/mole). The corrosion current density is related to the used fuel corrosion potential by the Tafel Equation (Equation3).

$$E_{CORR}^{Fuel} = E_A^0 + \frac{RT}{\alpha_A F} \ln \left(\frac{i_{CORR}}{nF\epsilon(SA)k_A} \right) \quad (Eq.13)$$

where E_{CORR}^{Fuel} is the corrosion potential (Volts), E_A^0 is the standard potential for Reaction A (see Table 1), α_A is the electrical charge transfer coefficient (related to Tafel slope for reaction of

interest), ε is the porosity of the U(VI) corrosion layer covering the used fuel surface (m^3 void/ m^3 corrosion phase), (SA) is the reactive surface area of the fuel (m^2), k_A is the rate constant for Reaction A (see Table 1), and R, T, F, n are the ideal gas constant, absolute temperature, Faraday constant and the number of electrons transferred respectively. As implied in Figure 5, the used fuel corrosion potential is also a function (E_0) of the concentrations of species involved in the oxidative dissolution of uranium (see Table 2 for reactions).

$$E_{\text{CORR}}^{\text{Fuel}} = E_0([\text{CO}_3^{2-}], [\text{O}_2], [\text{H}_2\text{O}_2], [\text{H}_2]) \quad (\text{Eq.14})$$

The relationships between reaction currents (directly proportional to reaction rates), rate constants, standard potentials and the corrosion potential for individual half-cell reactions at the used fuel surface (Table 2, Figure 4) are derived from the Tafel equations and quantified as follows:

$$i_A = nF\varepsilon k_A \exp\left[\frac{\alpha_A F}{RT} (E_{\text{CORR}}^{\text{Fuel}} - E_A^0)\right] \quad (\text{Eq.15})$$

$$i_B = nF\varepsilon k_B [\text{CO}_3^{2-}]^2 \exp\left[\frac{\alpha_B F}{RT} (E_{\text{CORR}}^{\text{Fuel}} - E_B^0)\right] \quad (\text{Eq.16})$$

$$i_C = nF\varepsilon k_C [\text{H}_2\text{O}_2] \exp\left[\frac{\alpha_C F}{RT} (E_{\text{CORR}}^{\text{Fuel}} - E_C^0)\right] \quad (\text{Eq.17})$$

$$-i_D = nF\varepsilon k_D [\text{H}_2\text{O}_2] \exp\left[\frac{-\alpha_D F}{RT} (E_{\text{CORR}}^{\text{Fuel}} - E_D^0)\right] \quad (\text{Eq.18})$$

$$-i_E = nF\varepsilon k_E [\text{O}_2] \exp\left[\frac{-\alpha_E F}{RT} (E_{\text{CORR}}^{\text{Fuel}} - E_E^0)\right] \quad (\text{Eq.19})$$

$$i_L = nF\varepsilon k_L [\text{H}_2] \exp\left[\frac{-\alpha_L F}{RT} (E_{\text{CORR}}^{\text{Fuel}} - E_L^0)\right] \quad (\text{Eq.20})$$

where $E_{\text{CORR}}^{\text{Fuel}}$ is the corrosion potential (Volts), E_A^0 is the standard potential for Reaction A (see Table 2), α_A is the electrical charge transfer coefficient (related to Tafel slope for reaction of interest), ε is the porosity of the U(VI) corrosion layer covering the used fuel surface (m^3 void/ m^3 corrosion phase), S is the reactive surface area of the fuel (m^2), k_A is the rate constant for Reaction A (see Table 2), and R, T, F, n are the ideal gas constant, absolute temperature, Faraday's constant and the number of electrons transferred respectively. Note that the equations are written with positive currents for anodic reactions and negative currents for cathodic reactions.

It follows from Equations Eq.21 - Eq.23 that the corrosion current densities for each half cell reaction can also be calculated based on the fluxes of key redox species (see Eq.1 - Eq.10 above for reaction-diffusion relationships):

$$2i_C + i_E = -nF\tau_f\varepsilon D_{O_2} \frac{\partial C_{O_2}(0,t)}{\partial x} \quad (\text{Eq.21})$$

$$i_C - i_D = -nF\tau_f\varepsilon D_{H_2O_2} \frac{\partial C_{H_2O_2}(0,t)}{\partial x} \quad (\text{Eq.22})$$

$$i_B = -nF\tau_f\varepsilon D_{UO_2(CO_3)_2^{2-}} \frac{\partial C_{UO_2(CO_3)_2^{2-}}(0,t)}{\partial x} \quad (\text{Eq.23})$$

$$i_A = -nF\tau_f\varepsilon D_{UO_2^{2+}} \frac{\partial C_{UO_2^{2+}}(0,t)}{\partial x} \quad (\text{Eq.24})$$

$$i_L = -nF\tau_f\varepsilon D_{H_2} \frac{\partial C_{H_2}(0,t)}{\partial x} \quad (\text{Eq.25})$$

where τ_f and ε are the tortuosity and porosity of the U(VI) corrosion layer, D is the diffusion coefficient and C is the molar concentration, x is the distance from the used fuel surface (Figure 2) and (0,t) refers to the partial derivative of concentration at $x = 0$ and time = t.

The fundamental axiom on which kinetic mixed potential theory models (such as the ANL-MPM) is thus quantified by the Equation 26 (see Reactions A - L, Table 2):

$$i_A + i_B + i_L - i_C - i_D - i_E = 0 \quad (\text{Eq.26})$$

Electrochemical and mass-flux relationships of the types written for the UO_2 surface (Eq.11-Eq.26) can also be written for the iron (steel) surface. See King and Kolar, 1999 for a complete treatment of the steel boundary surface.

2.3. Temperature Dependence of Rates and Key Parameter Values

The temperature dependence of the used fuel degradation rate is captured in the ANL-MPM using Arrhenius relationships for rate constants (Eq.27), saturation concentrations (Eq.28) and diffusion coefficients (Eq.29). A linear temperature dependency is used for standard electrochemical potentials (Eq.30).

$$k_i = k_i(T_r) \exp \left[\frac{\Delta H_i}{R} \left(\frac{1}{T_r} - \frac{1}{T} \right) \right] \quad (\text{Eq.27})$$

$$C_i^{\text{sat}} = C_i^{\text{sat}}(T_r) \exp \left[\frac{\Delta H_i^{\text{sat}}}{R} \left(\frac{1}{T_r} - \frac{1}{T} \right) \right] \quad (\text{Eq.28})$$

$$D_i = D_i(T_r) \exp \left[\frac{\Delta H_{D_i}}{R} \left(\frac{1}{T_r} - \frac{1}{T} \right) \right] \quad (\text{Eq.29})$$

$$E_i^0 = E_i^0(T_r) + \Delta E_i^0(T - T_r) \quad (\text{Eq.30})$$

where k is a rate constant, T_r is the reference temperature used in determining the activation energy (ΔH) and temperature dependence of the standard potential for a given half-cell reaction (ΔE^0), R is the ideal gas constant, C^{sat} is the molar concentration at which a given corrosion phase precipitates ($\text{UO}_3 \cdot 2\text{H}_2\text{O}$ for corrosion of fuel surface), and D_i is the diffusion coefficient for component i .

The temperature dependence of the dissolution of the iron corrosion product layer (reaction k_7) is more complicated and is not within the scope of this report since our focus was on UO_2 dissolution. For more details of the temperature dependence of iron corrosion see page 14 of King et al., 1999.

2.4. Treatment of Radiolysis and Generation of Radiolytic Oxidants (H_2O_2 only in ANL-MPM Version 1)

The spatial and temporal dependence of the alpha dose rate ($[\mathbf{R}_D(\mathbf{x},t) = R_{\text{scale}} R_{\text{aq}}(t)g(x)]$, see Table 3, Figure 5 for explanation) is of fundamental significance within the ANL-MPM Version 1 because, at low concentrations of dissolved oxygen, the only oxidant within the system is the hydrogen peroxide produced by alpha radiolysis. Therefore the rate of matrix degradation in anoxic environments (granite repository, deep bore-hole, etc.) is directly proportional to the alpha dose rate.

Calculating the alpha dose rate (and thus H_2O_2 concentration) for corroding UO_2 fuel is complicated by the effects of U(VI) corrosion products (modeled as schoepite, $\text{UO}_3 \cdot 2\text{H}_2\text{O}$ in ANL-MPM Version 1). A U(VI) corrosion product layer has four effects on the rate of UO_2 degradation:

- Corrosion layer can slow the rate of oxidative dissolution by decreasing the reactive surface area of the fuel (blocking or masking reaction sites).
- Corrosion layer can slow the rate of oxidative dissolution by blocking alpha-particles from interacting with water and producing radiolytic oxidants (decreases total moles H_2O_2 produced near fuel surface). The magnitude of this effect would be proportional to surface coverage of corrosion layer.
- Corrosion layer can slow the rate of oxidative dissolution by slowing the rate of diffusion of oxidants to the fuel surface: U(VI) layer is a tortuous porous mass of crystals.

- Corrosion layer can increase the rate of oxidative dissolution if alpha-emitting radionuclides (e.g., actinides) are incorporated into the U(VI) corrosion crystals or occluded within the mass of corrosion products.

All three of these effects are modeled in the ANL-MPM Version 1 by a radiolysis "sub-routine" that was included within the original Canadian-MPM (King and Kolar, 1999). Because of dependence of the used fuel dissolution rate on the alpha dose rate the radiolysis "sub-routine" is described in some detail. The MATLAB implementation of the radiolysis part of the ANL-MPM Version 1 is given in Appendix 2, lines 165 -209.

In the ANL-MPM Version 1 alpha-particles are assumed to have a constant energy of 5.3MeV and a solution penetration distance (α_{PEN}) of approximately 35 μm . The modeler can set the penetration distance over the range of $\alpha_{PEN} = 45\mu\text{m}$ for $\sim 6.0\text{MeV}$ alpha-particles down to $\alpha_{PEN} = 10\mu\text{m}$ for $\sim 2.3\text{ MeV}$ particles (King and Kolar, 1999). The quantity of hydrogen peroxide produced by alpha-radiolysis per unit of absorbed dose ($G_{\text{H}_2\text{O}_2}$) in both models is assumed to be $1.021\text{E-}10\text{ mol/Gy cm}^3$ (Christensen and Sunder, 2000).

Table 3. Parameters describing radiolysis (generation of H_2O_2) in the ANL-MPM Version 1 (adapted from King and Kolar, 1999).

Parameter	Symbol	Value	Units
G-value for the primary a-radiolysis yield of H_2O_2	$G_{\text{H}_2\text{O}_2}$	1.02E-10	mol/Gy cm^3
Time-dependent alpha dose rate to the solution	$R_{\text{aq}}(t)$	From fuel burn-up and history	----
Spatial- and time dependent alpha-radiation dose rate $R_{\text{D}}(\mathbf{x},t) = R_{\text{scale}} R_{\text{aq}}(t)g(\mathbf{x})$	$R_{\text{D}}(\mathbf{x},t)$	Calculated within MPM	----
Ratio of dose rate from U(VI) corrosion layer to dose rate from fuel	R_{film}	0 - 1	----
Geometrical factor describing a-radiation field	$g_i(\mathbf{x})$	Based on parameter inputs, see Fig. 5	----
a-particle penetration depth in water	a_{pen}	35	mm
Scaling factor for dose rate: for sensitivity runs	R_{scale}	1	----

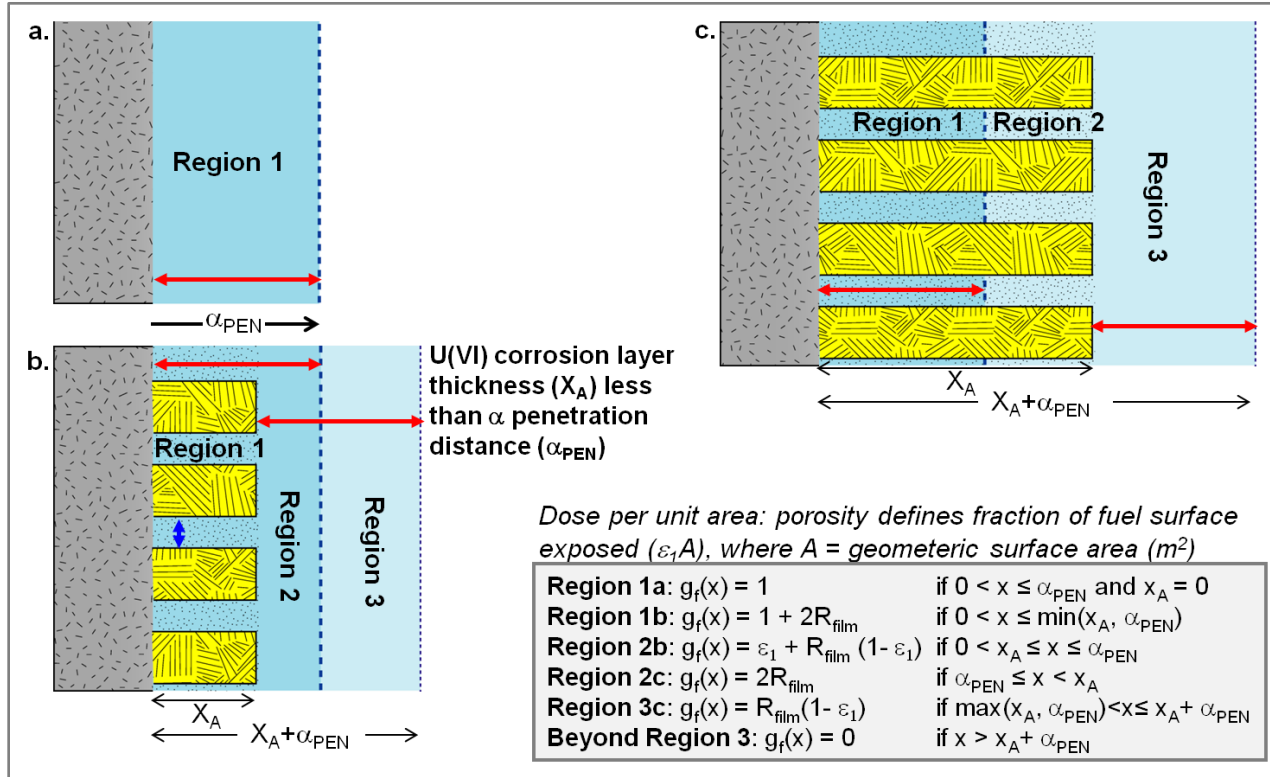


Figure 5. Conceptual rendering of the parallel pore model used for the treatment of radiolysis (H_2O_2 generation) in the ANL-MPM Version 1, as adapted from the Canadian-MPM of King and Kolar, 1999). See Table 3 for an explanation of the relationship used to determine the spatial- and temporal dose rate: $R_D(x,t) = R_{aq}(t)g(x)$. Red lines indicate alpha particle penetration distances for different scenarios.

The relationships shown conceptually in Figure can be summarized as follows:

- The spatial dependence of the a-dose rate and the effects of the precipitate film (corrosion layer) on the effective dose rate are taken into account. A number of regions at the corroded fuel surface need to be considered.
- Precipitated film (corrosion layer) is modeled as medium consisting of parallel pores have bulk porosity ϵ_1 and effective pore cross-sectional surface are of $\epsilon_1 A$ where A is the geometrical surface area.
- Region 1b: $x_A \leq \alpha_{pen}$ solution within pores is irradiated by fuel and walls of pores: effective dose per unit area $R_D(x,t) = \epsilon_1 R_{aq}(x,t)(1+2R_{film})$ [accounts for fact that only pore solution irradiated: $\epsilon_1 R_{aq}(x,t)$],
- Region 2b: $x_A < x \leq \alpha_{pen}$ the solution (beyond film surf) is irradiated by exposed fuel ($\epsilon_1 A$) and by the surf. of the film $A(1 - \epsilon_1)$: effective dose per unit area $R_D(x,t) = R_{aq}(x,t) [\epsilon_1 + R_{film}(1 - \epsilon_1)]$,
- Region 2c: $\alpha_{pen} \leq x < x_A$ the solution (beyond α_{pen} within pores) is irradiated only by the pore internal surfaces $A(1 - \epsilon_1)$: effective dose per unit area $R_D(x,t) = \epsilon_1 R_{aq}(x,t) 2R_{film}$,

- Region 3c: $X_A < x \leq (X_A + \alpha_{\text{pen}})$ the solution is irradiated by the surface of the porous film of cross-sectional area $A(1 - \epsilon_1)$: the effective dose per unit area $R_D(x,t) = R_{\text{aq}}(x,t) R_{\text{film}}(1 - \epsilon_1)$.

3. MATHEMATICAL IMPLEMENTATION OF ANL-MPM VERSION 1: SUMMARY

The ANL-MPM Version 1 is based on a set of ordinary differential equations in which concentrations are the state variables (Equations 1 - 10). Based on the relationships shown in Equations 1 - 26, and given a set of initial concentration values for key species at the used fuel surface, a corrosion potential is calculated such that the total current flow at that surface is zero (this is the fundamental axiom of mixed potential theory, Eq.26). The overall rates for all surface reactions are then calculated at that corrosion potential. The rates of the surface reactions control the flux of chemical species from the surface into solution. A species flux from the fuel surface is used to update the concentrations in the solution at the interfacial boundary. The cycle of calculations is repeated for the desired length of time.

The general flow of inputs and calculations involved in the ANL-MPM Version 1 is shown in Figure 6. MATLAB release R2012a, for a 64-bit platform was used to implement the ANL-MPM Version 1. Implementation of the ANL-MPM Version 1 is summarized as follows:

- Several well tested, built-in mathematical tools available in MATLAB were used to facilitate rapid model implementation.
- The time derivatives of the species identified in Equations 1 - 10 were calculated explicitly to reduce the model to a system of ordinary differential equations. The MATLAB environment allows for fully explicit and fully implicit, differencing schemes to be used in solving the reaction-diffusion problems.
- An adaptive time-step algorithm determines the length of a given time step based on the concentration gradients that form in the model during the course of a simulation
- Modeling systems of partial differential equations (Equations 1 - 10) requires discretization in order to calculate approximate derivative values. Appendix 2, which shows the MATLAB code for implementation of the ANL-MPM Version 1, describes the scheme used for discretization of the reaction-diffusion equations in x and t . Algebraic equations are derived from the discretization procedure and solved using standard MATLAB tools. Equations 1 - 10 are each solved at a grid point for each time interval t (by default there are 250 solution points, however, this number can be changed by the user: see Appendix 2, lines 52 to 80).
- The temperature and radioactive dose histories are functions of time that are supplied explicitly as an argument to the MPM and are not a result of the calculations (King and Kolar, 1999, King and Kolar, 2003 and references therein).
- Placeholder values for physical constants that are not explicitly documented in the Canadian-MPM (e.g., reaction rates and diffusivities) were used to implement the model. The relevant physical constants will be updated based on analyses of literature data and from on-going electrochemical experiments.

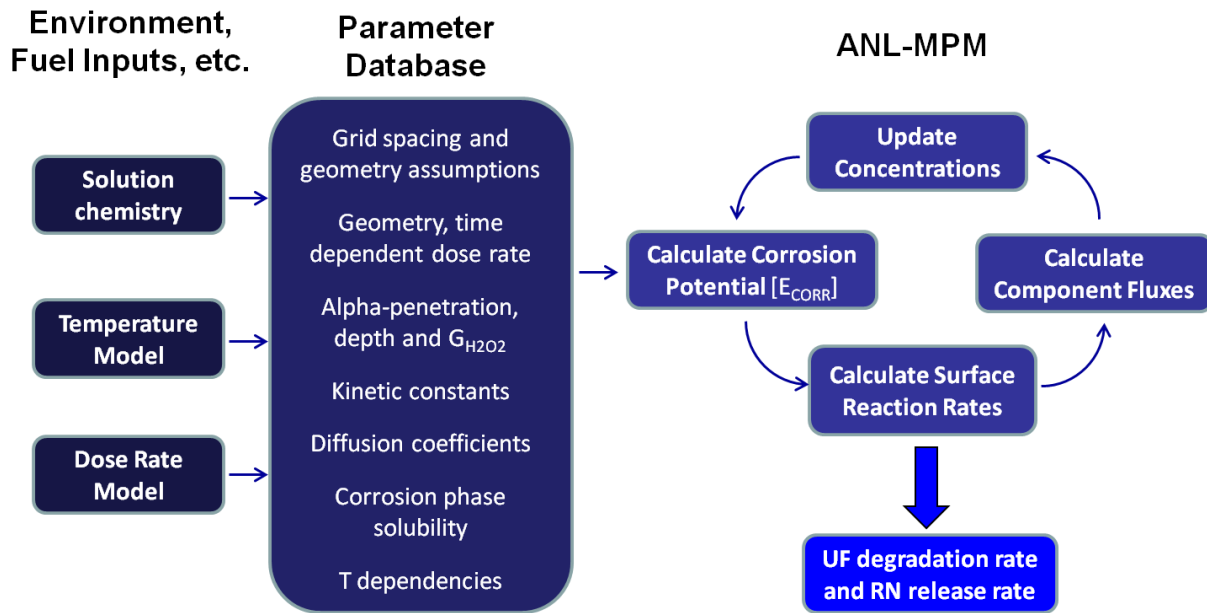


Figure 6. Conceptual drawing for the evolution of the used fuel corrosion potential and interfacial reaction rates with time as calculated by the ANL-MPM Version 1: see Appendix 2 for MATLAB scripts used to implement model.

4. SUMMARY AND FUTURE WORK

The purpose of this work is to develop and optimize a predictive model for the degradation of used uranium oxide fuel that is based on fundamental electrochemical and thermodynamic principals. This process model will be integrated with the UFD generic performance assessment model to provide a source term for radionuclide release for a disposal scenario of interest. The approach has been to implement, optimize and extend an existing, well tested electrochemical corrosion model to specific fuel degradation processes and mechanisms of interest.

Some of the specific multi-year objectives for this project that have been achieved thus far include:

- Implemented, using our own scripts/code (in MATLAB environment), an established and well documented used fuel degradation model (Canadian-mixed potential model) that is based on mixed potential theory (this report, see Appendices 1 and 2 for details on ANL MATLAB scripts).
- Verified our scripting and coding by reproducing published results from the Canadian model (Jerden et al., 2012).
- Performed sensitivity analyses to determine which model parameters and input variables have the strongest impact on the calculated used fuel degradation rate (Jerden et al., 2012).
- Completed a critical review of the sources of all model parameters and input variables to determine which values need further investigation through literature review or experimental studies. This review also identified which variables must be provided by other process models (Jerden et al., 2012).
- Extended the base-case model to quantify the role of dissolved hydrogen in protecting used fuel from oxidative dissolution by lowering the electrochemical potential at the fuel surface (Jerden et al., 2012).
- Developed a plan to extend the base-case model to account for the catalytic effects of fission product alloy phase (noble metal particles) on reactions affecting UO_2 dissolution, such as the kinetic balance of H_2 oxidation and H_2O_2 reduction (Jerden et al., 2012).

This work has provided a working, base-line model that is being modified and extended to include additional reactions and factors affecting fuel dissolution. The initial version of the MATLAB implementation of mixed potential model, referred to as the ANL-MPM Version 1, was verified by reproducing published results from the Canadian-MPM reports (Jerden et al., 2012). This report provides a detailed discussion of the actual coding that was used in the implementation of ANL-MPM Version 1. This report thus documents the base-line ANL-MPM on which future versions will be based.

This report presents the details of the first version of our UO_2 fuel matrix degradation model. The model described was produced by implementing the Canadian-mixed potential model for UO_2 fuel dissolution (King and Kolar, 1999, King and Kolar, 2003, Shoesmith et al., 2003) using the numerical computing environment and programming language MATLAB (release R2012a on 64-bit platform). The intent of the initial version was to reproduce the approach used by King and Kolar, 1999 to gain experience with the model, identify key model parameters to be

measured experimentally or determined from evaluation of the literature, and provide a touchstone for future modifications of the code.

The initial version of the MATLAB implementation of mixed potential model, referred to as the ANL-MPM Version 1, was verified by reproducing published results from the Canadian-MPM reports (Jerden et al., 2012). This report provides a detailed discussion of the actual coding that was used in the implementation of ANL-MPM Version 1.

The ANL-MPM Version 1 (MATLAB implementation of the Canadian-MPM described by King and Kolar, 1999) is a 1-dimensional reaction-diffusion model that accounts for the following processes:

- Interfacial redox reaction kinetics influencing oxidative dissolution of the UO_2 matrix.
- Chemical or solubility based dissolution of the fuel matrix.
- Complexation of dissolved uranium by carbonate near the fuel surface and in the bulk solution.
- Production of hydrogen peroxide (which is the dominant fuel oxidant in anoxic repository environments) by alpha-radiolysis.
- Diffusion of reactants and products in the groundwater away from and towards the reacting fuel surface.
- Precipitation and dissolution of a U-bearing corrosion product layer on the fuel surface.
- Adsorption of uranium onto iron oxides.
- Arrhenius-type temperature dependence for all interfacial and bulk reactions.

The ANL-MPM Version 1 will be used as a base-line check for future versions of the ANL-MPM. A working beta version of the ANL-MPM Version 2 has been implemented and is now being tested and optimized. The ANL-MPM Version 2 accounts for the following processes and conditions (in addition to processes listed above):

- Quantifies the oxidation of dissolved H_2 at the used fuel/solution interface: H_2 concentration to be supplied by other EBS model or user specified).
- Represents the NMPs as a separate domain at the used fuel/solution interface. The "size" of the NMP domain (relative to the fuel) is specified by the user in terms of a surface coverage and is electrically linked with the UO_2 matrix by a user adjustable resistance. This will allow the effects of NMP corrosion and sorption on the catalytic efficiency to be taken into account.
- Quantifies the bulk decomposition of hydrogen peroxide (with temperature dependence).
- Provides option for user to specify temperature and dose profiles of the fuel (profiles can be constant single values or functions).
- Includes Rapid diffusion option to facilitate the calculation of concentrations of species whose diffusion coefficients are sufficiently large that they reach steady state on the order of days (decreases computer time needed for model convergence).

This report focuses on the base-line model ANL-MPM Version 1; for a discussion of the conceptual basis for the ANL-MPM Version 2 see Jerden et al., 2012.

Because the ANL-MPM is based on fundamental principles, it is flexible enough to be applied to the full range of repository environments as well as shorter-term storage scenarios being considered as part of the UFD campaign. On-going experimental work described in Jerden et al., 2012 and Ebert et al., 2012 is focused on providing key model parameter values that are needed to improve predictive accuracy and capabilities of the ANL-MPM.

5. REFERENCES CITED AND CONSULTED

Christensen, H. and Sunder, S. (2000). "Current State of Knowledge of Water Radiolysis Effects on Spent Nuclear Fuel Corrosion." *Nuclear Technology*, 131, (1), 102-123.

Ebert, W. L., Cruse, T. A., and Jerden J., (2012), "Electrochemical Experiments Supporting Oxide Fuel Corrosion Model" U.S. Department of Energy Used Fuel Disposition Campaign, Argonne National Laboratory Milestone Report FCRD-UFD-2012-000201

Jerden, J., Fortner, J., Cruse, T., Cunnane, J. (2011). *Repository Science/Waste Form Degradation & Radionuclide Mobilization*, Prepared for U.S. Department of Energy Used Fuel Disposition Campaign, Argonne National Laboratory Milestone Report M41UF030701 for the work package: FTAN11UF0307, July, 2011.

Jerden, J., Fortner, J., Cruse, T., Frey, K., Ebert, W., (2012). *Experimental Plan for ANL Electrochemical Corrosion Studies*, Prepared for U.S. Department of Energy Used Fuel Disposition Campaign, Argonne National Laboratory Milestone Report FCRD-USED-2012-000, January 6, 2012

Jerden, J., Frey, K., Cruse, T., and Ebert, W. (2012a). *Waste Form Degradation Model Status Report: Electrochemical Model for Used Fuel Matrix Degradation Rate*. FCRD-UFD-2012-000169.

King, F. and Kolar, M. (1999) "Mathematical Implementation of the Mixed-Potential Model of Fuel Dissolution Model Version MPM-V1.0", Ontario Hydro, Nuclear Waste Management Division Report No. 06819-REP-01200-10005 R00.

King, F. and Kolar, M. (2002) "Validation of the Mixed-Potential Model for Used Fuel Dissolution Against Experimental Data", Ontario Hydro, Nuclear Waste Management Division Report No. 06819-REP-01200-10077-R00.

King, F. and Kolar, M. (2003) "The Mixed-Potential Model for UO₂ Dissolution MPM Versions V1.3 and V1.4", Ontario Hydro, Nuclear Waste Management Division Report No. 06819-REP-01200-10104 R00.

Sassani et al., 2012 *"Integration of EBS Models with Generic Disposal System Models"*, U.S. Department of Energy, Used Fuel Disposition Campaign milestone report: M2FT-12SN0806062, September, 7 2012

Shoesmith, D.W., S. Sunder, M. G. Bailey, and G. J. Wallace (1989). "The Corrosion of Nuclear Fuel (UO₂) in Oxygenated Solutions." *Corrosion Science*, 29, 1115-1128.

Shoesmith, D.W., S. Sunder, and J. C. Tait (1998). "Validation of an Electrochemical Model for the Oxidative Dissolution of Used CANDU Fuel." *Journal of Nuclear Materials*, 257, 89-98.

Shoesmith, D.W. (2000). "Fuel Corrosion Processes Under Waste Disposal Conditions." *Journal of Nuclear Materials*, 282, 1-31.

Shoesmith, D.W., M. Kolar, and F. King (2003). "A Mixed-Potential Model to Predict Fuel (Uranium Dioxide) Corrosion Within a Failed Nuclear Waste Container" *Corrosion*, 59, 802-816.

Shoesmith, D. W. (2007). *Used Fuel and Uranium Dioxide Dissolution Studies – A Review*. NWMO TR-2007-03, July 2007 Nuclear Waste Management Organization, 22 St. Clair Avenue East, 6th Floor, Toronto, Ontario M4T 2S3, Canada.

Shoesmith, D. W. (2008). *The Role of Dissolved Hydrogen on the Corrosion/Dissolution of Spent Nuclear Fuel*, NWMO TR-2008-19, November 2008 Nuclear Waste Management Organization, 22 St. Clair Avenue East, 6th Floor, Toronto, Ontario M4T 2S3, Canada.

Sunder, S., N.H. Miller, D.W. Shoesmith, (2004). "Corrosion of uranium dioxide in hydrogen peroxide solutions" *Corrosion Science*, 46, 1095–1111.

UFD R&D Roadmap (2011). *Used Fuel Disposition Campaign Disposal Research and Development Roadmap*. FCRD-USED-2011-000065 REV0, March 2011.

Appendix 1

Input parameter summary for ANL-MPM Version 1 for MATLAB (release R2012a). Black text is copied directly from MATLAB scripts, green text are comments in the code.

```
1      F = 96487; % C/mol
2      R = 8.314; % J/mol/K
3      L = 0.05; % m distance fuel - steel
4      nPts = 250; Number of grid points
5      t = 1*365*24*60*60; % s time of simulation
6
7      D(MPM_data.UO2) = 0.5e-09*exp(15000*dT); % m^2/s
8      D(MPM_data.UCO3) = 0.5e-09*exp(15000*dT); % m^2/s
9      D(MPM_data.Uads) = 0.1e-10*exp(15000*dT); % m^2/s
10     D(MPM_data.Usus) = 0.1e-09*exp(15000*dT); % m^2/s
11     D(MPM_data.CO3) = 1.7e-09*exp(15000*dT); % m^2/s
12     D(MPM_data.O2) = 1.7e-09*exp(15000*dT); % m^2/s
13     D(MPM_data.H2O2) = 1.7e-09*exp(15000*dT); % m^2/s
14     D(MPM_data.Fe2) = 0.5e-09*exp(15000*dT); % m^2/s
15     D(MPM_data.UO3) = 0.1e-10*exp(15000*dT); % m^2/s
16     D(MPM_data.FeO) = 0.1e-10*exp(15000*dT); % m^2/s
17     D(MPM_data.H2) = 4.5e-09*exp(15000*dT); % m^2/s
18
19     M(MPM_data.UO2) = 0.302; % kg/mol
20     M(MPM_data.UCO3) = 0.422; % kg/mol
21     M(MPM_data.Uads) = 0.302; % kg/mol
22     M(MPM_data.Usus) = 0.270; % kg/mol
23     M(MPM_data.CO3) = 0.060; % kg/mol
24     M(MPM_data.O2) = 0.032; % kg/mol
25     M(MPM_data.H2O2) = 0.034; % kg/mol
26     M(MPM_data.Fe2) = 0.056; % kg/mol
27     M(MPM_data.UO3) = 0.322; % kg/mol
28     M(MPM_data.FeO) = 0.232; % kg/mol
29     M(MPM_data.H2) = 0.002; % kg/mol
30
31     rho(1) = 4980; % kg/m^3; U(VI) corrosion layer (Schoepite) (ID = 1)
32     rho(2) = 1000; % kg/m^3; Bulk water layer (ID = 2)
33     rho(3) = 5173; % kg/m^3; Iron oxide corrosion layer (ID = 3)
34
35     epsl(1) = 0.45; % U(VI) corrosion layer (Schoepite)
36     epsl(2) = 1.00; % Water layer
37     epsl(3) = 0.10; % Iron oxide corrosion layer
38
39     tau(1) = 0.10; % U(VI) corrosion layer (Schoepite) (ID = 1)
40     tau(2) = 1.00; % Bulk water layer (ID = 2)
41     tau(3) = 0.10; % Iron oxide corrosion layer (ID = 3)
42
43     G = 1.021e-4; % generation value in mol/(J/kg)/m^3
44     penD = 3.5e-5; % alpha particle penetration distance in m
45     Rf = 1.0; % Factor for dose from corrosion film
46     dR = 0.02 % Constant dose rate (J/kg)/s
47
48     T = 298.15 % constant temperature in K
49
50     Cs(MPM_data.UO2,:) = 3.20e-2*exp(6e4*dT); % mol/m^3
```

```
51 Cs (MPM_data.UCO3,:) = 4.67e-2*exp(6e4*dT)*...
52 (conc(MPM_data.CO3)^1.34); % mol/m^3
53 Cs (MPM_data.Uads,:) = 5.0e-3*(rho(3)*eps1(3)); % mol/m^3
54 Cs (MPM_data.Fe2,:) = 1.00e-2*exp(6e4*dT); % mol/m^3
55
56 Cinit(MPM_data.CO3) = 1.0e-6; % mol/m^3
57 Cinit(MPM_data.O2) = 1.0e-6; % mol/m^3
58
59 % One entry per half reaction at fuel surface
60 % cMat: number of electrons generated
61 % kMat: reaction rate constant (mol/m^3/s; or appropriate)
62 % ectc: electrochemical charge transfer coefficient
63 % oMat: reaction order in concentrations
64 % sMat: stoichiometry matrix
65 % Ezero: standard potential (Vsce)
66
67 %*****%
68 % Fuel 1: Reaction A %
69 % Fuel -> UO2(2+) + 2e(-) %
70 %*****%
71 cMat(1,1) = 2;
72 kMat(1,1) = 5.0e-8*exp(6.0e4*dT);
73 ectc(1,1) = 0.96;
74 Ezero(1,1) = 0.169 - 0.000248*(T-298);
75
76 %*****%
77 % Fuel 2: Reaction B %
78 % Fuel + 2CO3(2-) -> UO2(CO3)2(2-) + 2e(-) %
79 %*****%
80 cMat(2,1) = 2;
81 kMat(2,1) = 1.43e-12 *exp(6.0e4*dT);
82 ectc(2,1) = 0.82;
83 Ezero(2,1) = -0.173 + 0.002100*(T-298);
84
85 %*****%
86 % Fuel 3: Reaction C %
87 % H2O2 -> O2 + 2H(+) + 2e(-) %
88 %*****%
89 cMat(3,1) = 2;
90 kMat(3,1) = 7.4e-8 *exp(6.0e4*dT);
91 ectc(3,1) = 0.41;
92 Ezero(3,1) = -0.121 - 0.000993*(T-298);
93
94 %*****%
95 % Fuel 4: Reaction D %
96 % H2O2 + 2e(-) -> 2OH(-) %
97 %*****%
98 cMat(4,1) = -2;
99 kMat(4,1) = 1.2e-12 *exp(6.0e4*dT);
100 ectc(4,1) = -0.41;
101 Ezero(4,1) = 0.973 - 0.000698*(T-298);
102
103 %*****%
104 % Fuel 5: Reaction E %
105 % O2 + 2H2O + 4e(-) -> 4OH(-) %
106 %*****%
```

```
107      cMat(5,1) = -4;
108      kMat(5,1) = 1.4e-12 *exp(6.0e4*dT);
109      ectc(5,1) = -0.50;
110      Ezero(5,1) = 0.426 - 0.000123*(T-298);
111
112      %*****%
113      % Container 1: Reaction F          %
114      % UO2(2+) + 2e(-) -> UO2        %
115      %*****%
116      cMat(1,1) = -2;
117      kMat(1,1) = 1.00e-9 *exp(6.0e4*dT);
118      ectc(1,1) = -0.50;
119      Ezero(1,1) = 0.169 - 0.000248*(T-298);
120
121      %*****%
122      % Container 2: Reaction G          %
123      % UO2(CO3)2(2-) + 2e(-) -> UO2 + 2CO3(2-) %
124      %*****%
125      cMat(2,1) = -2;
126      kMat(2,1) = 1.00e-10 *exp(6.0e4*dT);
127      ectc(2,1) = -0.50;
128      Ezero(2,1) = -0.173 + 0.002100*(T-298);
129
130      %*****%
131      % Container 3: Reaction H          %
132      % H2O2 + 2e(-) -> 2OH(-)        %
133      %*****%
134      cMat(3,1) = -2;
135      kMat(3,1) = 1.6e-14 *exp(6.0e4*dT);
136      ectc(3,1) = -0.38;
137      Ezero(3,1) = 0.973 - 0.000698*(T-298);
138
139      %*****%
140      % Container 4: Reaction I          %
141      % O2 + 2H2O + 4e(-) -> 4OH(-)    %
142      %*****%
143      cMat(4,1) = -4;
144      kMat(4,1) = 3.2e-12 *exp(6.0e4*dT);
145      ectc(4,1) = -0.42;
146      Ezero(4,1) = 0.426 - 0.000123*(T-298);
147
148      %*****%
149      % Container 5: Reaction J          %
150      % Container -> Fe(2+) + 2e(-)    %
151      %*****%
152      cMat(5,1) = 2;
153      kMat(5,1) = 2.2e-5*exp(10.4e4*dT);
154      ectc(5,1) = 1.08;
155      Ezero(5,1) = -0.650 + 0.000680*(T-298);
156
157      %*****%
158      % Container 6: Reaction K          %
159      % H2O + e(-) -> (1/2)H2 + OH(-)  %
160      %*****%
161      cMat(6,1) = -1;
162      kMat(6,1) = 1.2e-7 *exp(5.21e4*dT);
```

```
163      ectc(6,1) = -0.48;
164      Ezero(6,1) = -0.802 - 0.001900*(T-298);
165
166      %*****%
167      % Bulk 1: Reaction 1 %
168      % UO2(2+) + 2OH(-) + H2O -> UO3*2H2O %
169      %*****%
170      kMat(1,1) = 1e-3*exp(6.0e4*dT);
171
172      %*****%
173      % Bulk 2: Reaction 2f %
174      % UO2(CO3)2(2-) + 2OH(-) + H2O -> UO3*2H2O + 2CO3(2-) %
175      %*****%
176      kMat(2,1) = 1e-4*exp(6.0e4*dT);
177
178      %*****%
179      % Bulk 3: Reaction 2r %
180      % UO3*2H2O + 2CO3(2-) -> UO2(CO3)2(2-) + 2OH(-) + H2O %
181      %*****%
182      kMat(3,1) = 6.3e-12*exp(6.0e4*dT);
183
184      %*****%
185      % Bulk 4: Reaction 3 %
186      % O2 + 4Fe(2+) + 8OH(-) -> 4H2O + 2Fe2O3 %
187      %*****%
188      kMat(4,1) = 5.9e-1*exp(6.0e4*dT);
189
190      %*****%
191      % Bulk 5: Reaction 4 %
192      % H2O2 + 2Fe(2+) + 4OH(-) -> 3H2O + Fe2O3 %
193      %*****%
194      kMat(5,1) = 6.9e-2*exp(4.2e4*dT);
195
196      %*****%
197      % Bulk 6: Reaction 5 %
198      % UO2(2+) + 2Fe(2+) + 6OH(-) -> UO2 + 3H2O + Fe2O3 %
199      %*****%
200      kMat(6,1) = 1.0e-2*exp(6.0e4*dT);
201
202      %*****%
203      % Bulk 7: Reaction 6 %
204      % UO2(CO3)2(2-) + 2Fe(2+) + 6OH(-) -> UO2 + 2CO3(2-) + 3H2O + Fe2O3 %
205      %*****%
206      kMat(7,1) = 1.0e-3*exp(6.0e4*dT);
207
208      %*****%
209      % Bulk 8: Reaction 7f %
210      % Fe(2+) + 2OH(-) -> (1/3)Fe3O4 + (2/3)H2O + (1/3)H2 %
211      %*****%
212      kMat(8,1) = 1.0e-3*exp(6.0e4*dT);
213
214      %*****%
215      % Bulk 9: Reaction 7r %
216      % (1/3)Fe3O4 + (2/3)H2O + (1/3)H2 -> Fe(2+) + 2OH(-) %
217      %*****%
```



```
218         kMat(9,1) = 0;
219
220         %*****%
221         % Bulk 10: Reaction 8f (adsorption) %
222         % UO2(2+) -> UO2(2+) %
223         %*****%
224         kMat(10,1) = 1e-6*exp(0.0*dT);
225
226         %*****%
227         % Bulk 11: Reaction 8r (desorption) %
228         % UO2(2+) -> UO2(2+) %
229         %*****%
230         kMat(11,1) = 1e-9*exp(0.0*dT);
231
232         %*****%
233         % Bulk 12: Reaction 9f (adsorption) %
234         % UO2(CO3)2(2-) -> UO2(2+) + 2CO3(2-) %
235         %*****%
236         kMat(12,1) = 1e-9*exp(0.0*dT);
237
238         %*****%
239         % Bulk 13: Reaction 9r (desorption) %
240         % UO2(2+) + 2CO3(2-) -> UO2(CO3)2(2-) %
241         %*****%
242         kMat(13,1) = 1e-9*exp(0.0*dT);
```

Appendix 2

MATLAB scripts for implementation of the ANL-MPM Version 1 (MATLAB release R2012a). Black text is active code, green text are comments in the code. The ANL-MPM Version 1 for MATLAB consists of five individual files that must be in the MATLAB operational folder to run the model. The code is presented in the following order below:

The **MPM_data** file is a data container that holds information on simulation time steps, grid spacing, temperature, dose rate, H₂O₂ generation, species stoichiometry, saturation concentrations, diffusion coefficients, porosity, tortuosity of corrosion layer etc.

The **MPM_react** file defines the reactions and calculates the rates of reactions and corrosion potentials at the fuel surface (and container surface if included). Probably the most important file since the corrosion potential is the defining characteristic of the model. This file is called recursively when calculating the corrosion potential. This file also defines the reactions and calculates the rates of reactions that occur in the space between the fuel surface and end of domain (end of domain can be iron canister or bulk solution).

The **MPM_main** file is a top level function that calls all the other files needed to run the ANL-MPM Version 1.

The **MPM_odefun** file provides input arguments to the MATLAB ordinary differential equation solver.

The **MPM_odestat** file provides the status function and reshape of matrix for the MATLAB ordinary differential equation solver.

The **MPM_output** file writes data to a comma separated value file.

1 This file: **MPM_data**, is a data container that holds information on simulation time steps, grid
2 spacing, temperature, dose rate, H₂O₂ generation, species stoichiometry, saturation
3 concentrations, diffusion coefficients, porosity, tortuosity of corrosion layer etc.
4

```
5 %Start MATLAB script
6
7 classdef MPM_data < uint16I
8
9     enumeration
10        % Enumeration of component list (members of MATLAB class here defined)
11        UO2      (1)    % UO2 (2+)      (aqueous)
12        UCO3     (2)    % UO2(CO3)2 (2-) (aqueous)
13        Uads     (3)    % UO2 (2+)      (adsorbed on solid iron corrosion)
14        Usus    (4)    % UO2          (homogeneous solid suspension)
15        CO3      (5)    % CO3 (2-)      (aqueous)
16        O2       (6)    % O2           (aqueous)
17        H2O2     (7)    % H2O2        (aqueous)
18        Fe2      (8)    % Fe (2+)     (aqueous)
19        UO3      (9)    % UO3*2H2O   (solid uranium corrosion product)
20        FeO      (10)   % Fe3O4      (solid iron corrosion product)
21        H2       (11)   % H2          (aqueous)
22
23        % Components not tracked by code: produced in bulk / at surfaces;
24        %      (XX)    % Fe2O3      (homogeneous solid suspension)
25        %      (XX)    % H (+)      (aqueous)
26        %      (XX)    % OH (-)    (aqueous)
27    end
28
29    methods(Static)II
30
31        % Faraday's constant
32        function F = constF()
33            F = 96487; % C/mol
34        end
35
36        % Gas constant
37        function R = constR()
38            R = 8.314; % J/mol/K
39        end
40
41        % Number of components
42        function nCmps = cmpList()
43            [~, compNames] = enumeration('MPM_data');
44            nCmps = length(compNames);
45        end
46
```

^I **classdef**: begins the class definition. There are many different data types, or classes, in MATLAB. You can build matrices and arrays of floating-point and integer data, characters and strings, and logical true and false states.

^{II} **static methods** are associated with a class, but not with specific instances of that class. These methods do not perform operations on individual objects of a class and, therefore, do not require an instance of the class as an input argument, like ordinary methods. Static methods are useful when you do not want to first create an instance of the class before executing some code. For example, you might want to set up the MATLAB environment or use the static method to calculate data needed to create class instances.

```
47     % Dimension of environment, distance from fuel surf to steel surf
48     function L = cellLen()
49         L = 0.05; % m
50     end
51
52     % Number of grid points used
53     function nPts = gridPts()
54         nPts = 250;
55     end
56
57     % Grid subdivisions
58     function lmat = ordVec()
59         % Retrieve constants
60         cellLen = MPM_data.cellLen();
61         gridPts = MPM_data.gridPts();
62
63         % Spacing parameter
64         sp = 0;
65
66         % Symmetric, logspace grid
67         hp = floor(gridPts/2);
68         df = 2*(10^sp)/cellLen;
69         x1 = (logspace(-3, sp, hp)-1e-3)/df; x1(1) = 0;
70         IL = x1(end)-x1(end-1);
71         if(hp == gridPts/2)
72             mf = (x1(end)-IL/2)/x1(end);
73             x1 = x1*mf;
74             lmat = [x1, cellLen-fliplr(x1)];
75         else
76             mp = x1(end); mf = (x1(end)-IL)/x1(end);
77             x1 = x1*mf;
78             lmat = [x1, mp, cellLen-fliplr(x1)];
79         end
80     end
81
82     % Duration of simulation
83     function t = maxTime()
84         t = 1*365*24*60*60; % s
85     end
86
87     % Diffusion coefficients
88     % T (K): temperature; scalar
89     function D = valD(T)
90         % Retrieve constants
91         R = MPM_data.constR();
92         nCmps = MPM_data.cmpList();
93         dT = (1/298-1/T)/R;
94
95         % Default to 1e-9 m^2/s
96         D = zeros(nCmps,1) + 1e-9;
97
98         % Data
99         D(MPM_data.UO2) = 0.5e-09*exp(15000*dT); % m^2/s
100        D(MPM_data.UCO3) = 0.5e-09*exp(15000*dT); % m^2/s
101        D(MPM_data.Uads) = 0.1e-10*exp(15000*dT); % m^2/s
```

```
102     D(MPM_data.Usus) = 0.1e-09*exp(15000*dT);    % m^2/s
103     D(MPM_data.CO3) = 1.7e-09*exp(15000*dT);    % m^2/s
104     D(MPM_data.O2)  = 1.7e-09*exp(15000*dT);    % m^2/s
105     D(MPM_data.H2O2) = 1.7e-09*exp(15000*dT);    % m^2/s
106     D(MPM_data.Fe2) = 0.5e-09*exp(15000*dT);    % m^2/s
107     D(MPM_data.UO3) = 0.1e-10*exp(15000*dT);    % m^2/s
108     D(MPM_data.FeO) = 0.1e-10*exp(15000*dT);    % m^2/s
109     D(MPM_data.H2)  = 4.5e-09*exp(15000*dT);    % m^2/s
110 end
111
112 % Molecular weights
113 function M = molWT()
114     % Retrieve constants
115     nCmps = MPM_data.cmpList();
116
117     % Default to 0.018 kg/mol
118     M = zeros(nCmps,1) + 0.018; % kg/mol
119
120     % Data
121     M(MPM_data.UO2) = 0.302; % kg/mol
122     M(MPM_data.UCO3) = 0.422; % kg/mol
123     M(MPM_data.Uads) = 0.302; % kg/mol
124     M(MPM_data.Usus) = 0.270; % kg/mol
125     M(MPM_data.CO3) = 0.060; % kg/mol
126     M(MPM_data.O2)  = 0.032; % kg/mol
127     M(MPM_data.H2O2) = 0.034; % kg/mol
128     M(MPM_data.Fe2) = 0.056; % kg/mol
129     M(MPM_data.UO3) = 0.322; % kg/mol
130     M(MPM_data.FeO) = 0.232; % kg/mol
131     M(MPM_data.H2)  = 0.002; % kg/mol
132 end
133
134 % Porosities
135 function epsl = poro()
136     % Data
137     epsl(1) = 0.45; % U(VI) corrosion layer (Schoepite)
138     epsl(2) = 1.00; % Water layer
139     epsl(3) = 0.10; % Iron oxide corrosion layer
140 end
141
142 % Tortuosities
143 function tau = tort()
144     tau(1) = 0.10; % U(VI) corrosion layer (Schoepite) (ID = 1)
145     tau(2) = 1.00; % Bulk water layer (ID = 2)
146     tau(3) = 0.10; % Iron oxide corrosion layer (ID = 3)
147 end
148
149 % Layer densities
150 function rho = dens()
151     rho(1) = 4980; % kg/m^3; U(VI) corrosion layer (Schoepite) (ID = 1)
152     rho(2) = 1000; % kg/m^3; Bulk water layer (ID = 2)
153     rho(3) = 5173; % kg/m^3; Iron oxide corrosion layer (ID = 3)
154 end
155
156 % Region identification
```

```

157     % conc (M): concentrations; matrix
158     function [corr0,corrL] = regID(conc)
159     % Retrieve constants
160     MW      = MPM_data.molWT();
161     eps1    = MPM_data.poro();
162     rho     = MPM_data.dens();
163     lmat    = MPM_data.ordVec();
164
165     % Calculate corrosion products mass per square meter of surface area
166     %U(VI) corrosion layer (Schoepite)
167     tot0 = trapz(lmat,conc(MPM_data.UO3,:))*MW(MPM_data.UO3);III % kg/m^2
168     % Iron oxide corrosion layer
169     totL = trapz(lmat,conc(MPM_data.FeO,:))*MW(MPM_data.FeO); % kg/m^2
170
171     % Determine layer thickness
172     %U(VI) corrosion layer (Schoepite)
173     corr0 = tot0/(rho(1)*(1-eps1(1)+eps)); % m
174     % Iron oxide corrosion layer
175     corrL = totL/(rho(3)*(1-eps1(3)+eps)); % m
176     end
177
178     % ANL-MPM V 1 Radiolysis model for peroxide generation
179     % t(s):      time; scalar
180     % conc(M):  concentrations; matrix
181     function [rGen,dR] = alphRad(t,conc)
182     % Retrieve constants
183     lmat      = MPM_data.ordVec();
184     corr0     = MPM_data.regID(conc);
185     eps1      = MPM_data.poro();
186
187     % Radiolysis data
188     G        = 1.021e-4; % generation value in mol/(J/kg)/m^3
189     penD     = 3.5e-5; % alpha particle penetration distance in m
190     Rf       = 1.0;IV % Factor for dose from corrosion film
191
192     % Empirical correlation of dose history from King and Kolar, 1999 p.74
193     %xdat = [3.092e7 1.615e8 3.113e9 2.708e10 3.134e11 3.156e13];
194     %ydat = [1.929e-2 1.313e-2 1.929e-2 1.051e-2 3.590e-3 6.504e-5];
195     %dR = interp1(xdat,ydat,t,'linear','extrap'); % (J/kg)/s
196     dR = 0.02 % Constant dose rate (J/kg)/s
197
198     % Form factor calc, accounts effect of corrosion layer geometry on dose
199     FF      = zeros(1,length(lmat));
200     r1 = (lmat >= 0)&(lmat <= penD);
201     r2 = (lmat >= corr0)&(lmat <= corr0+penD);
202     r3 = (lmat > 0)&(lmat < corr0);
203
204     FF(r1) = FF(r1) + ( eps1(1));
205     FF(r2) = FF(r2) + (1-eps1(1))*Rf;
206     FF(r3) = FF(r3) + ( eps1(1))*Rf*2;

```

^{III} **Z = trapz(X,Y)** computes the integral of Y with respect to X using trapezoidal integration. Inputs X and Y can be complex.

^{IV} **Rf** is the dose ratio of U(VI) corrosion layer / fuel, based on assumption of incorporation of alpha emitting radionuclides into corrosion layer. Rf = 1.0 indicates dose from corrosion layer equivalent to dose from fuel (dR).

```

207
208     % Rate expression for peroxide generation
209     rGen = G*dR*FF; % mol/m^3/s
210 end
211
212 % Temperature
213 % t (s): time; scalar
214 function T = temp(t)
215     % Empirical correlation of T history from King and Kolar, 1999 p.39
216     %log_sec = min(log(t+3e5),29.5);
217     %a = [21.9 41.3 890 72.61 -488 ];
218     %b = [20.27 18.43 44.53 25.72 29.92];
219     %c = [ 1.46 3.267 35.98 4.027 11.41];
220     %T = sum(a.*exp(-((log_sec-b)./c).^2)); % K
221     T = 298.15 % constant temperature in K
222 end
223
224 % Saturation concentrations
225 % T (K): temperature; scalar
226 % conc (M): concentrations; matrix
227 function Cs = satVals(T,conc)
228     %Retrieve constants
229     R = MPM_data.constR();
230     nCmps = MPM_data.cmpList();
231     nPts = MPM_data.gridPts();
232     rho = MPM_data.dens();
233     epsl = MPM_data.poro();
234     dT = (1/298-1/T)/R;
235
236     % Default to 10000 mol/m^3
237     Cs = zeros(nCmps,nPts) + 1e4;
238
239     % Data
240     Cs(MPM_data.UO2,:) = 3.20e-2*exp(6e4*dT); % mol/m^3
241     Cs(MPM_data.UCO3,:) = 4.67e-2*exp(6e4*dT)*...
242         (conc(MPM_data.CO3)^1.34); % mol/m^3
243     Cs(MPM_data.Uads,:) = 5.0e-3*(rho(3)*epsl(3)); % mol/m^3
244     Cs(MPM_data.Fe2,:) = 1.00e-2*exp(6e4*dT); % mol/m^3
245 end
246
247 % Initial concentrations
248 function Cinit = initVals()
249     % Retrieve constants
250     nCmps = MPM_data.cmpList();
251
252     % Default to 0.0 mol/m^3
253     Cinit = zeros(nCmps,1);
254
255     % Data
256     Cinit(MPM_data.CO3) = 1.0e-6; % mol/m^3
257     Cinit(MPM_data.O2) = 1.0e-6; % mol/m^3
258     Cinit(MPM_data.H2O2) = 0; % mol/m^3
259     Cinit(MPM_data.UO3) = 0.5e+0;
260 end
261 end

```

262 [end](#)

263 This file: **MPM_react** defines the reactions and calculates the rates of reactions and corrosion
 264 potentials at the fuel surface (and container surface if included). Probably the most important file
 265 since the corrosion potential is the defining characteristic of the model. This file is called
 266 recursively when calculating the corrosion potential. This file also defines the reactions and
 267 calculates the rates of reactions that occur in the space between the fuel surface and end of
 268 domain (end of domain can be iron canister or bulk solution).

```

269 %Start MATLAB script
270
271
272 function [Rvec,sMat,oFun,dFun,Ecorr]V = MPM_react(rSet,t,conc,Ecorr)
273
274 % Initialize parameters
275 [nCmps,nPts] = size(conc);
276 sMat         = zeros(nCmps,0);
277 oFun         = 0;
278 dFun         = 0;
279
280 % Retrieve constants
281 F            = MPM_data.constF();
282 R            = MPM_data.constR();
283 T            = MPM_data.temp(t);
284
285 % Calculate temperature dependence
286 dT          = (1/298-1/T)/R;
287
288 % Calculate reaction set
289 switch(rSet)
290 % Fuel surface reactions
291 case 1
292 % Calculate corrosion potential (recursive)
293 if(nargin<4)VI
294 Ecorr = 0; dEcorr = 1;
295 [~,~,oFun,dFun] = MPM_react(rSet,t,conc,Ecorr);
296 while(abs(dEcorr) > 1e-3 && abs(Ecorr) < 10)VII
297 dEcorr = min(oFun/dFun,5);VIII
298 oFunTest = 2*abs(oFun); dFunTest = 0; EcorrNew = 0;
299 while(abs(oFunTest)>abs(oFun))
300
301 EcorrNew = Ecorr - dEcorr;
302 [~,~,oFunTest,dFunTest] = MPM_react(rSet,t,conc,EcorrNew);
303 dEcorr = dEcorr/2;
304 end
305 Ecorr = EcorrNew;
306 oFun = oFunTest; dFun = dFunTest;
307 end
308 end
309
  
```

^V **Rvec**: vector of reaction rates, **sMat**: stoichiometry matrix, **oFun**: objective function, **dFun**: derivative function, **Ecorr**: corrosion potential (Vsce)

^{VI} **nargin<4** returns the number of input arguments passed in the call to the currently executing function.

^{VII} **abs(X)** returns an array Y such that each element of Y is the absolute value of the corresponding element of X.

^{VIII} **C = min(A)** returns the smallest elements along different dimensions of an array.

```
310 %*****%
311 % Start Fuel Reactions %
312 %*****%
313
314 % One entry per half reaction at fuel surface
315 % cMat: number of electrons generated
316 % kMat: reaction rate constant (mol/m^3/s; or appropriate)
317 % ectc: electrochemical charge transfer coefficient
318 % oMat: reaction order in concentrations
319 % sMat: stoichiometry matrix
320 % Ezero: standard potential (Vsce)
321
322 %*****%
323 % Fuel 1: Reaction A %
324 % Fuel -> UO2(2+) + 2e(-) %
325 %*****%
326
327 oMat = zeros(nCmps,1);
328 sMatAdd = zeros(nCmps,1);
329
330 cMat(1,1) = 2;
331 kMat(1,1) = 5.0e-8 *exp(6.0e4*dT);
332 ectc(1,1) = 0.96;
333 Ezero(1,1) = 0.169 - 0.000248*(T-298);
334
335 sMatAdd(MPM_data.UO2) = 1;
336 sMat = [sMat,sMatAdd];
337 cDep(1,1) = prod(conc.^oMat);
338
339 %*****%
340 % Fuel 2: Reaction B %
341 % Fuel + 2CO3(2-) -> UO2(CO3)2(2-) + 2e(-) %
342 %*****%
343
344 oMat = zeros(nCmps,1);
345 sMatAdd = zeros(nCmps,1);
346
347 cMat(2,1) = 2;
348 kMat(2,1) = 1.43e-12 *exp(6.0e4*dT);
349 ectc(2,1) = 0.82;
350 Ezero(2,1) = -0.173 + 0.002100*(T-298);
351
352 sMatAdd(MPM_data.CO3) = -2;
353 sMatAdd(MPM_data.UCO3) = 1;
354 sMat = [sMat,sMatAdd];
355 oMat(MPM_data.CO3) = 0.66;
356 cDep(2,1) = prod(conc.^oMat);
357
358 %*****%
359 % Fuel 3: Reaction C %
360 % H2O2 -> O2 + 2H(+) + 2e(-) %
361 %*****%
362
363 oMat = zeros(nCmps,1);
364 sMatAdd = zeros(nCmps,1);
```

```
365
366     cMat(3,1) = 2;
367     kMat(3,1) = 7.4e-8 *exp(6.0e4*dT);
368     ectc(3,1) = 0.41;
369     Ezero(3,1) = -0.121 - 0.000993*(T-298);
370
371
372     sMatAdd(MPM_data.H2O2) = -1;
373     sMatAdd(MPM_data.O2) = 1;
374     sMat = [sMat, sMatAdd];
375     oMat(MPM_data.H2O2) = 1;
376     cDep(3,1) = prod(conc.^oMat);
377
378     %*****%
379     % Fuel 4: Reaction D %
380     % H2O2 + 2e(-) -> 2OH(-) %
381     %*****%
382
383     oMat = zeros(nCmps,1);
384     sMatAdd = zeros(nCmps,1);
385
386     cMat(4,1) = -2;
387     kMat(4,1) = 1.2e-12 *exp(6.0e4*dT);
388     ectc(4,1) = -0.41;
389     Ezero(4,1) = 0.973 - 0.000698*(T-298);
390
391     sMatAdd(MPM_data.H2O2) = -1;
392     sMat = [sMat, sMatAdd];
393     oMat(MPM_data.H2O2) = 1;
394     cDep(4,1) = prod(conc.^oMat);
395
396     %*****%
397     % Fuel 5: Reaction E %
398     % O2 + 2H2O + 4e(-) -> 4OH(-) %
399     %*****%
400
401     oMat = zeros(nCmps,1);
402     sMatAdd = zeros(nCmps,1);
403
404     cMat(5,1) = -4;
405     kMat(5,1) = 1.4e-12 *exp(6.0e4*dT);
406     ectc(5,1) = -0.50;
407     Ezero(5,1) = 0.426 - 0.000123*(T-298);
408
409     sMatAdd(MPM_data.O2) = -1;
410     sMat = [sMat, sMatAdd];
411     oMat(MPM_data.O2) = 1;
412     cDep(5,1) = prod(conc.^oMat);
413
414     %*****%
415     % End Fuel Reactions %
416     %*****%
417
418     % Vector of reaction rates, objective function, derivative
```

```

419         Rvec =          kMat.*cDep.*exp(ectc*F/R/T.*(Ecorr-Ezero));
420         oFun = sum(cMat.*kMat.*cDep.*exp(ectc*F/R/T.*(Ecorr-Ezero)));
421         dFun = sum(cMat.*ectc*F/R/T.*Rvec);
422
423     % Container surface reactions
424     case 2
425         % Calculate corrosion potential (recursive)
426         if(nargin<4)
427             Ecorr = 9.5; dEcorr = 1;
428             [~,~,oFun,dFun] = MPM_react(rSet,t,conc,Ecorr);
429             while(abs(dEcorr) > 1e-3 && abs(Ecorr) < 10)
430                 dEcorr = min(oFun/dFun,5);
431                 oFunTest = 2*abs(oFun); dFunTest = 0; EcorrNew = 0;
432                 while(abs(oFunTest)>abs(oFun))
433                     EcorrNew = Ecorr - dEcorr;
434                     [~,~,oFunTest,dFunTest] = MPM_react(rSet,t,conc,EcorrNew);
435                     dEcorr = dEcorr/2;
436                 end
437                 Ecorr = EcorrNew;
438                 oFun = oFunTest; dFun = dFunTest;
439             end
440         end
441
442         %*****%
443         % Start Container Reactions          %
444         %*****%
445
446         % One entry per half reaction at container surface
447         %   cMat:  number of electrons generated
448         %   kMat:  reaction rate constant (mol/m^3/s; or appropriate)
449         %   ectc:  electrochemical charge transfer coefficient
450         %   oMat:  reaction order in concentrations
451         %   sMat:  stoichiometry matrix
452         %   Ezero: standard potential (Vsce)
453
454         %*****%
455         % Container 1: Reaction F          %
456         % UO2(2+) + 2e(-) -> UO2          %
457         %*****%
458
459         oMat          = zeros(nCmps,1);
460         sMatAdd       = zeros(nCmps,1);
461
462         cMat(1,1)    = -2;
463         kMat(1,1)    = 1.00e-9 *exp(6.0e4*dT);
464         ectc(1,1)    = -0.50;
465         Ezero(1,1)   = 0.169 - 0.000248*(T-298);
466
467         sMatAdd(MPM_data.UO2)    = -1;
468         sMatAdd(MPM_data.Usus)   = 1;
469         sMat                     = [sMat,sMatAdd];
470         oMat(MPM_data.UO2)       = 1;
471         cDep(1,1)                = prod(conc.^oMat);
472
473         %*****%

```

```
474      % Container 2: Reaction G                                %
475      % UO2(CO3)2(2-) + 2e(-) -> UO2 + 2CO3(2-)           %
476      %*****%
477
478      oMat                = zeros(nCmps,1);
479      sMatAdd             = zeros(nCmps,1);
480
481      cMat(2,1) = -2;
482      kMat(2,1) = 1.00e-10 *exp(6.0e4*dT);
483      ectc(2,1) = -0.50;
484      Ezero(2,1) = -0.173 + 0.002100*(T-298);
485
486      sMatAdd(MPM_data.CO3) = 2;
487      sMatAdd(MPM_data.Usus) = 1;
488      sMatAdd(MPM_data.UCO3) = -1;
489      sMat = [sMat,sMatAdd];
490      oMat(MPM_data.UCO3) = 1;
491      cDep(2,1) = prod(conc.^oMat);
492
493      %*****%
494      % Container 3: Reaction H                                %
495      % H2O2 + 2e(-) -> 2OH(-)                               %
496      %*****%
497
498      oMat                = zeros(nCmps,1);
499      sMatAdd             = zeros(nCmps,1);
500
501      cMat(3,1) = -2;
502      kMat(3,1) = 1.6e-14 *exp(6.0e4*dT);
503      ectc(3,1) = -0.38;
504      Ezero(3,1) = 0.973 - 0.000698*(T-298);
505
506      sMatAdd(MPM_data.H2O2) = -1;
507      sMat = [sMat,sMatAdd];
508      oMat(MPM_data.H2O2) = 1;
509      cDep(3,1) = prod(conc.^oMat);
510
511      %*****%
512      % Container 4: Reaction I                                %
513      % O2 + 2H2O + 4e(-) -> 4OH(-)                         %
514      %*****%
515
516      oMat                = zeros(nCmps,1);
517      sMatAdd             = zeros(nCmps,1);
518
519      cMat(4,1) = -4;
520      kMat(4,1) = 3.2e-12 *exp(6.0e4*dT);
521      ectc(4,1) = -0.42;
522      Ezero(4,1) = 0.426 - 0.000123*(T-298);
523
524      sMatAdd(MPM_data.O2) = -1;
525      sMat = [sMat,sMatAdd];
526      oMat(MPM_data.O2) = 1;
527      cDep(4,1) = prod(conc.^oMat);
```

```

528
529 %*****%
530 % Container 5: Reaction J %
531 % Container -> Fe(2+) + 2e(-) %
532 %*****%
533
534 oMat = zeros(nCmps,1);
535 sMatAdd = zeros(nCmps,1);
536
537 cMat(5,1) = 2;
538
539 % kMat(5,1) = 2.2e-5*exp(10.4e4*dT);
540 kMat(5,1) = 0.0; % Turns off iron reactions
541
542 ectc(5,1) = 1.08;
543 Ezero(5,1) = -0.650 + 0.000680*(T-298);
544
545 sMatAdd(MPM_data.Fe2) = 1;
546 sMat = [sMat,sMatAdd];
547 cDep(5,1) = prod(conc.^oMat);
548
549 %*****%
550 % Container 6: Reaction K %
551 % H2O + e(-) -> (1/2)H2 + OH(-) %
552 %*****%
553
554 oMat = zeros(nCmps,1);
555 sMatAdd = zeros(nCmps,1);
556
557 cMat(6,1) = -1;
558 kMat(6,1) = 1.2e-7 *exp(5.21e4*dT);
559 ectc(6,1) = -0.48;
560 Ezero(6,1) = -0.802 - 0.001900*(T-298);
561
562 sMatAdd(MPM_data.H2) = 1;
563 sMat = [sMat,sMatAdd];
564 cDep(6,1) = prod(conc.^oMat);
565
566 %*****%
567 % End Container Reactions %
568 %*****%
569
570 % Vector of reaction rates, objective function, derivative
571 Rvec = kMat.*cDep.*exp(ectc*F/R/T.*(Ecorr-Ezero));
572 oFun = sum(cMat.*kMat.*cDep.*exp(ectc*F/R/T.*(Ecorr-Ezero)));
573 dFun = sum(cMat.*ectc*F/R/T.*Rvec);
574
575 % Bulk reactions
576 case 3
577 % Corrosion layer thicknesses
578 [~,corrL] = MPM_data.regID(conc);
579 lmat = MPM_data.ordVec();
580 cellL = MPM_data.cellLen();
581 cLL = (lmat > (cellL-corrL));

```

```
582
583 % Saturation concentrations
584 Csat = MPM_data.satVals(T, conc);
585 Csat(MPM_data.Uads, :) = Csat(MPM_data.Uads, :).*cLL;
586
587 % Sub and supersaturation concentrations
588 concSub = max(Csat - conc, 0);
589 concSup = max(conc - Csat, 0);
590
591 %*****%
592 % Start Bulk Reactions %
593 %*****%
594
595 % One entry per bulk reaction
596 % kMat: reaction rate constant (mol/m^3/s; or appropriate)
597 % oMat: reaction order in concentrations
598 % oMatSub: reaction order in subsaturation
599 % oMatSup: reaction order in supersaturation
600 % sMat: stoichiometry matrix
601
602 %*****%
603 % Bulk 1: Reaction 1 %
604 % UO2(2+) + 2OH(-) + H2O -> UO3*2H2O %
605 %*****%
606
607 oMat = zeros(nCmps, 1);
608 oMatSub = zeros(nCmps, 1);
609 oMatSup = zeros(nCmps, 1);
610 sMatAdd = zeros(nCmps, 1);
611
612 kMat(1,1) = 1e-3*exp(6.0e4*dT);
613
614 oMatSup(MPM_data.UO2) = 1;
615 sMatAdd(MPM_data.UO2) = -1;
616 sMatAdd(MPM_data.UO3) = 1;
617 sMat = [sMat, sMatAdd];
618 cDep(1, :) = prod(conc.^ repmat(oMat, 1, nPts), 1).*...
619 prod(concSub.^ repmat(oMatSub, 1, nPts), 1).*...
620 prod(concSup.^ repmat(oMatSup, 1, nPts), 1);
621
622 %*****%
623 % Bulk 2: Reaction 2f %
624 % UO2(CO3)2(2-) + 2OH(-) + H2O -> UO3*2H2O + 2CO3(2-) %
625 %*****%
626
627 oMat = zeros(nCmps, 1);
628 oMatSub = zeros(nCmps, 1);
629 oMatSup = zeros(nCmps, 1);
630 sMatAdd = zeros(nCmps, 1);
631
632 kMat(2,1) = 1e-4*exp(6.0e4*dT);
633
634 oMatSup(MPM_data.UCO3) = 1;
635 sMatAdd(MPM_data.UCO3) = -1;
```

```
636     sMatAdd(MPM_data.CO3) = 2;
637     sMatAdd(MPM_data.UO3) = 1;
638     sMat = [sMat, sMatAdd];
639     cDep(2, :) = prod(conc.^ repmat(oMat, 1, nPts), 1) .* ...
640               prod(concSub.^ repmat(oMatSub, 1, nPts), 1) .* ...
641               prod(concSup.^ repmat(oMatSup, 1, nPts), 1);
642
643     %*****%
644     % Bulk 3: Reaction 2r %
645     % UO3*2H2O + 2CO3(2-) -> UO2(CO3)2(2-) + 2OH(-) + H2O %
646     %*****%
647
648     oMat = zeros(nCmps, 1);
649     oMatSub = zeros(nCmps, 1);
650     oMatSup = zeros(nCmps, 1);
651     sMatAdd = zeros(nCmps, 1);
652
653     kMat(3, 1) = 6.3e-12*exp(6.0e4*dT);
654
655     oMat(MPM_data.UO3) = 1;
656     sMatAdd(MPM_data.UO3) = 1;
657     sMatAdd(MPM_data.CO3) = -2;
658     sMatAdd(MPM_data.UO3) = -1;
659     sMat = [sMat, sMatAdd];
660     cDep(3, :) = prod(conc.^ repmat(oMat, 1, nPts), 1) .* ...
661                  prod(concSub.^ repmat(oMatSub, 1, nPts), 1) .* ...
662                  prod(concSup.^ repmat(oMatSup, 1, nPts), 1);
663
664     %*****%
665     % Bulk 4: Reaction 3 %
666     % O2 + 4Fe(2+) + 8OH(-) -> 4H2O + 2Fe2O3 %
667     %*****%
668
669     oMat = zeros(nCmps, 1);
670     oMatSub = zeros(nCmps, 1);
671     oMatSup = zeros(nCmps, 1);
672     sMatAdd = zeros(nCmps, 1);
673
674     kMat(4, 1) = 5.9e-1*exp(6.0e4*dT);
675
676     oMat(MPM_data.O2) = 1;
677     oMat(MPM_data.Fe2) = 1;
678     sMatAdd(MPM_data.O2) = -1;
679     sMatAdd(MPM_data.Fe2) = -4;
680     sMat = [sMat, sMatAdd];
681     cDep(4, :) = prod(conc.^ repmat(oMat, 1, nPts), 1) .* ...
682                  prod(concSub.^ repmat(oMatSub, 1, nPts), 1) .* ...
683                  prod(concSup.^ repmat(oMatSup, 1, nPts), 1);
684
685     %*****%
686     % Bulk 5: Reaction 4 %
687     % H2O2 + 2Fe(2+) + 4OH(-) -> 3H2O + Fe2O3 %
688     %*****%
689
690     oMat = zeros(nCmps, 1);
```



```
691         oMatSub           = zeros (nCmps, 1);
692         oMatSup           = zeros (nCmps, 1);
693         sMatAdd           = zeros (nCmps, 1);
694
695         kMat (5,1)  =    6.9e-2*exp (4.2e4*dT);
696
697         oMat (MPM_data.H2O2)   = 1;
698         oMat (MPM_data.Fe2)    = 1;
699         sMatAdd (MPM_data.H2O2) = -1;
700         sMatAdd (MPM_data.Fe2) = -2;
701         sMat           = [sMat, sMatAdd];
702         cDep (5, :)     = prod (conc.^ repmat (oMat, 1, nPts), 1) .* ...
703             prod (concSub.^ repmat (oMatSub, 1, nPts), 1) .* ...
704             prod (concSup.^ repmat (oMatSup, 1, nPts), 1);
705
706         %*****%
707         % Bulk 6: Reaction 5 %
708         % UO2(2+) + 2Fe(2+) + 6OH(-) -> UO2 + 3H2O + Fe2O3 %
709         %*****%
710
711         oMat           = zeros (nCmps, 1);
712         oMatSub        = zeros (nCmps, 1);
713         oMatSup        = zeros (nCmps, 1);
714         sMatAdd        = zeros (nCmps, 1);
715
716         kMat (6,1)  =    1.0e-2*exp (6.0e4*dT);
717
718         oMat (MPM_data.UO2)   = 1;
719         oMat (MPM_data.Fe2)    = 1;
720         sMatAdd (MPM_data.UO2) = -1;
721         sMatAdd (MPM_data.Fe2) = -1;
722         sMatAdd (MPM_data.Usus) = 1;
723         sMat           = [sMat, sMatAdd];
724         cDep (6, :)     = prod (conc.^ repmat (oMat, 1, nPts), 1) .* ...
725             prod (concSub.^ repmat (oMatSub, 1, nPts), 1) .* ...
726             prod (concSup.^ repmat (oMatSup, 1, nPts), 1);
727
728         %*****%
729         % Bulk 7: Reaction 6 %
730         % UO2(CO3)2(2-) + 2Fe(2+) + 6OH(-) -> UO2 + 2CO3(2-) + 3H2O + Fe2O3 %
731         %*****%
732
733         oMat           = zeros (nCmps, 1);
734         oMatSub        = zeros (nCmps, 1);
735         oMatSup        = zeros (nCmps, 1);
736         sMatAdd        = zeros (nCmps, 1);
737
738         kMat (7,1)  =    1.0e-3*exp (6.0e4*dT);
739
740         oMat (MPM_data.UCO3)   = 1;
741         oMat (MPM_data.Fe2)    = 1;
742         sMatAdd (MPM_data.UCO3) = -1;
743         sMatAdd (MPM_data.Fe2) = -2;
744         sMatAdd (MPM_data.Usus) = 1;
745         sMatAdd (MPM_data.CO3) = 2;
```

```

746     sMat                = [sMat,sMatAdd];
747     cDep(7,:)          = prod(conc.^ repmat(oMat, 1,nPts),1).*...
748                       prod(concSub.^repmat(oMatSub,1,nPts),1).*...
749                       prod(concSup.^repmat(oMatSup,1,nPts),1);
750
751     %*****%
752     % Bulk 8: Reaction 7f %
753     % Fe(2+) + 2OH(-) -> (1/3)Fe3O4 + (2/3)H2O + (1/3)H2 %
754     %*****%
755
756     oMat                = zeros(nCmps,1);
757     oMatSub             = zeros(nCmps,1);
758     oMatSup             = zeros(nCmps,1);
759     sMatAdd             = zeros(nCmps,1);
760
761     kMat(8,1)          = 1.0e-3*exp(6.0e4*dT);
762
763     oMatSup(MPM_data.Fe2) = 1;
764     sMatAdd(MPM_data.Fe2) = -1;
765     sMatAdd(MPM_data.FeO) = 1/3;
766     sMatAdd(MPM_data.H2)  = 1/3;
767     sMat                = [sMat,sMatAdd];
768     cDep(8,:)          = prod(conc.^ repmat(oMat, 1,nPts),1).*...
769                       prod(concSub.^repmat(oMatSub,1,nPts),1).*...
770                       prod(concSup.^repmat(oMatSup,1,nPts),1);
771
772     %*****%
773     % Bulk 9: Reaction 7r %
774     % (1/3)Fe3O4 + (2/3)H2O + (1/3)H2 -> Fe(2+) + 2OH(-) %
775     %*****%
776
777     oMat                = zeros(nCmps,1);
778     oMatSub             = zeros(nCmps,1);
779     oMatSup             = zeros(nCmps,1);
780     sMatAdd             = zeros(nCmps,1);
781
782     % Depreciated - Unreasonably fast
783     %vct1 = 10^(-8.794 - 1254/T - 3725/T*(Ecorr_contain+0.241));
784     %vct2 = 10^( 4.575 - 3970/T - 1753/T*(Ecorr_contain+0.241));
785     %vct3 = 10^(-5.772 - 2298/T - 876/T*(Ecorr_contain+0.241));
786     %kMat(9,1) = (vct3 + (vct2*vct1)/(vct2+vct1))*1e4;
787
788     kMat(9,1)          = 0;
789
790     oMat(MPM_data.FeO)   = 1;
791     sMatAdd(MPM_data.Fe2) = 1;
792     sMatAdd(MPM_data.FeO) = -1/3;
793     sMatAdd(MPM_data.H2)  = -1/3;
794     sMat                = [sMat,sMatAdd];
795     cDep(9,:)          = prod(conc.^ repmat(oMat, 1,nPts),1).*...
796                       prod(concSub.^repmat(oMatSub,1,nPts),1).*...
797                       prod(concSup.^repmat(oMatSup,1,nPts),1);
798
799     %*****%
800     % Bulk 10: Reaction 8f (adsorption) %

```

```
801      % UO2 (2+) -> UO2 (2+)          %
802      %*****%
803
804      oMat          = zeros (nCmps,1);
805      oMatSub       = zeros (nCmps,1);
806      oMatSup       = zeros (nCmps,1);
807      sMatAdd       = zeros (nCmps,1);
808
809      kMat (10,1)   = 1e-6*exp (0.0*dT);
810
811      oMat (MPM_data.UO2) = 1;
812      oMatSub (MPM_data.Uads) = 1;
813      sMatAdd (MPM_data.UO2) = -1;
814      sMatAdd (MPM_data.Uads) = 1;
815      sMat         = [sMat, sMatAdd];
816      cDep (10, :) = prod (conc.^ repmat (oMat, 1, nPts), 1) .* ...
817                      prod (concSub.^ repmat (oMatSub, 1, nPts), 1) .* ...
818                      prod (concSup.^ repmat (oMatSup, 1, nPts), 1);
819
820      %*****%
821      % Bulk 11: Reaction 8r (desorption) %
822      % UO2 (2+) -> UO2 (2+)          %
823      %*****%
824
825      oMat          = zeros (nCmps,1);
826      oMatSub       = zeros (nCmps,1);
827      oMatSup       = zeros (nCmps,1);
828      sMatAdd       = zeros (nCmps,1);
829
830      % ANL: Slowed down desorption
831      %kMat (11,1) = 1e-6*exp (0.0*dT);
832      kMat (11,1) = 1e-9*exp (0.0*dT);
833
834      oMat (MPM_data.Uads) = 1;
835      sMatAdd (MPM_data.UO2) = 1;
836      sMatAdd (MPM_data.Uads) = -1;
837      sMat         = [sMat, sMatAdd];
838      cDep (11, :) = prod (conc.^ repmat (oMat, 1, nPts), 1) .* ...
839                      prod (concSub.^ repmat (oMatSub, 1, nPts), 1) .* ...
840                      prod (concSup.^ repmat (oMatSup, 1, nPts), 1);
841
842      %*****%
843      % Bulk 12: Reaction 9f (adsorption) %
844      % UO2 (CO3)2 (2-) -> UO2 (2+) + 2CO3 (2-) %
845      %*****%
846
847      oMat          = zeros (nCmps,1);
848      oMatSub       = zeros (nCmps,1);
849      oMatSup       = zeros (nCmps,1);
850      sMatAdd       = zeros (nCmps,1);
851
852      kMat (12,1)   = 1e-9*exp (0.0*dT);
853
854      oMat (MPM_data.UCO3) = 1;
855      oMatSub (MPM_data.Uads) = 1;
```

```
856     sMatAdd(MPM_data.UCO3) = -1;
857     sMatAdd(MPM_data.Uads) = 1;
858     sMatAdd(MPM_data.CO3) = 2;
859     sMat = [sMat, sMatAdd];
860     cDep(12, :) = prod(conc.^ repmat(oMat, 1, nPts), 1) .* ...
861                 prod(concSub.^ repmat(oMatSub, 1, nPts), 1) .* ...
862                 prod(concSup.^ repmat(oMatSup, 1, nPts), 1);
863
864     %*****%
865     % Bulk 13: Reaction 9r (desorption) %
866     % UO2(2+) + 2CO3(2-) -> UO2(CO3)2(2-) %
867     %*****%
868
869     oMat = zeros(nCmps, 1);
870     oMatSub = zeros(nCmps, 1);
871     oMatSup = zeros(nCmps, 1);
872     sMatAdd = zeros(nCmps, 1);
873
874     % ANL: Changed to complex carbonate
875     % kMat(13,1) = 1e-6*exp(0.0*dT);
876     kMat(13,1) = 1e-9*exp(0.0*dT);
877
878     oMat(MPM_data.Uads) = 1;
879     oMat(MPM_data.CO3) = 1;
880     sMatAdd(MPM_data.UCO3) = 1;
881     sMatAdd(MPM_data.Uads) = -1;
882     sMatAdd(MPM_data.CO3) = -2;
883     sMat = [sMat, sMatAdd];
884     cDep(13, :) = prod(conc.^ repmat(oMat, 1, nPts), 1) .* ...
885                     prod(concSub.^ repmat(oMatSub, 1, nPts), 1) .* ...
886                     prod(concSup.^ repmat(oMatSup, 1, nPts), 1);
887
888     %*****%
889     % End Bulk Reactions %
890     %*****%
891
892     % Matrix of reation rates
893     Rvec = repmat(kMat, 1, nPts) .* cDep;
894
895     end
896
897     return
898
899
```

900 This file: **MPM_main**, is a top level function that calls all the other files needed to run the ANL-
901 MPM V 1.

```
902 %Start MATLAB script
903
904 function [] = MPM_main()
905
906     % Retrieves number of components
907     nCmps = MPM_data.cmpList();
908
909     % Simulation Parameters
910     cellLen = MPM_data.cellLen();
911     tmax     = MPM_data.maxTime();
912     gridPts = MPM_data.gridPts();
913     lmat     = MPM_data.ordVec();
914
915     % Define initial conditions
916     Cinit = MPM_data.initVals();
917     X0     = repmat(Cinit,1,gridPts);
918
919     % Group ordinary differential equation (ode) parameters
920     params.cellLen = cellLen;
921     params.gridPts = gridPts;
922     params.nCmps   = nCmps;
923     params.lmat    = lmat;
924
925     % Set ordinary differential equation (ode) options
926     opts = odeset('OutputFcn',@MPM_odestat,'NonNegative',1:(nCmps*gridPts));ix
927
928     % User feedback
929     clc;
930     fprintf(['Running ', '\n']);
931
932     % Performs simulation
933     [tvec,Xout] = ode15s(@MPM_odefun,[0.01 tmax],X0,opts,params);x
934
935     % Reshapes output matrices
936     tLen = length(tvec);
937     Xmat = zeros(tLen,gridPts,nCmps);
938     for k1 = 1:nCmps
939         Xmat(:, :, k1) = Xout(:, k1:nCmps:nCmps*gridPts);
940     end
941
942     % Create output report file
943     fprintf(['Writing Results', '\n']);
944     MPM_output(tvec, lmat, Xmat);
945
```

^{ix} The **odeset** function lets the user adjust the integration parameters of the relevant ordinary differential equation solvers.

^x **[tvec,Xout] = ode15s(@MPM_odefun, [0.01 tmax], X0,opts,params)** integrates the system of differential equations $y' = f(t,y)$ from time t_0 to t_f with initial conditions y_0 . Default integration parameters are replaced by property values specified in options, an argument created with the odeset function. The MATLAB ode15s solver is preferred for stiff problem types.

946

947 [return](#)

948 This file: **MPM_odefun** provides input arguments to the MATLAB ordinary differential
949 equation solver.

```
950 %Start MATLAB script
951
952 function [dt] = MPM_odefun(t,X,params)XI
953
954     % Unpack parameters
955     nCmps    = params.nCmps;
956     gridPts  = params.gridPts;
957     lmat     = params.lmat;
958
959     % Reshape inputs/outputs
960     X        = reshape(X,nCmps,gridPts);
961     dt       = zeros(nCmps,gridPts);
962
963     % Define finite difference ranges
964     r1 = 1;           % Fuel boundary
965     r2 = 2:gridPts-1; % Bulk
966     r3 = gridPts;    % Container boundary
967
968     % Interval size to the right
969     intVR      = zeros(1,gridPts);
970     intVR(1:end-1) = lmat(2:end)-lmat(1:end-1);
971     intVR(end)   = intVR(end-1);
972     intVR        = repmat(intVR,nCmps,1);
973
974     % Temperature, Diffusivity, Radiolysis
975     T          = MPM_data.temp(t);
976     D          = MPM_data.valD(T);
977     rGen       = MPM_data.alphRad(t,X);
978
979     % Initial Concentrations, Corrosion, Porosity
980     Cinit      = MPM_data.initVals();
981     [corr0,corrL] = MPM_data.regID(X);
982     epsl       = MPM_data.poro();
983
984     % Reaction rates
985     [Rvec0, sMat0] = MPM_react(1,t,X(:,1));
986     [RvecL, sMatL] = MPM_react(2,t,X(:,end));
987     [RvecBulk,sMatBulk] = MPM_react(3,t,X(:,:));
988
989     % Flux bounday conditions
990     dx0 = -epsl(2)*(sMat0*Rvec0)./(D+eps);
991     dxL = epsl(2)*(sMatL*RvecL)./(D+eps);
992
993     % Fixed boundary conditions
994     dx0([3,4,8:11]) = 0;
995     dxL(MPM_data.CO3) = (Cinit(MPM_data.CO3)-X(MPM_data.CO3,r3))/intVR(end);
996
997     % Bulk reactions
998
```

^{XI} **odefun**: A MATLAB function handle that evaluates the right side of the differential equations. Provides input arguments to MATLAB ordinary differential equation solvers.

```
999     rRates = sMatBulk*RvecBulk;
1000
1001     % Second derivatives
1002     dx2      = zeros(nCmps,gridPts);
1003     dx2(:,r1) = ((X(:,r1+1)-X(:,r1))./intVR(:,r1) - ...
1004                dx0
1005                (0.5*intVR(:,r1)
1006                ));
1007     dx2(:,r2) = ((X(:,r2+1)-X(:,r2))./intVR(:,r2) - ...
1008                (X(:,r2)-X(:,r2-1))./intVR(:,r2-1))./ ...
1009                (0.5*intVR(:,r2) + 0.5*intVR(:,r2-1)));
1010     dx2(:,r3) = (dxL
1011                (X(:,r3)-X(:,r3-1))./intVR(:,r3-1))./ ...
1012                (
1013                0.5*intVR(:,r3-1)));
1013
1014     % Diffusion contributions
1015     dt = dt + repmat(D,1,gridPts).*dx2;
1016
1017     % Reaction contributions
1018     dt = dt + rRates;
1019
1020     % Radiolysis Contributions
1021     dt(MPM_data.H2O2,:) = dt(MPM_data.H2O2,:) + rGen;
1022
1023     % Reshape outputs
1024     dt = reshape(dt,gridPts*nCmps,1);
1025
1026     return
1027
```


1028 This file: **MPM_odestat** provides the status function and reshape of matrix for the MATLAB
1029 ordinary differential equation solver.

```
1030  
1031 %Start MATLAB script  
1032  
1033 function [status] = MPM_odestat(t,X,flag,~)  
1034  
1035 % Continue evaluation  
1036 status = 0;  
1037  
1038 % Unpack parameters  
1039 nCmps = MPM_data.getCmpList();  
1040 gridPts = MPM_data.gridPts();  
1041  
1042 % Reshape inputs/outputs  
1043 if(isempty(flag))XII  
1044 X = reshape(X(:,1),nCmps,gridPts);XIII  
1045 end  
1046  
1047 % Output the time to the screen  
1048 if(isempty(flag))  
1049 clc;  
1050 fprintf(['Running ', '\n']);  
1051 fprintf('Time (sec) = %12.5E \n',t(end));  
1052 end  
1053  
1054 return  
1055
```

^{XII} Determines whether array flag is empty. **TF = isempty(A)** returns logical 1 (true) if A is an empty array and logical 0 (false) otherwise. An empty array has at least one dimension of size zero.

^{XIII} **X = reshape(A,m,n)** returns the m-by-n matrix B whose elements are taken column-wise from A. An error results if A does not have m*n elements.

1056 This file: **MPM_output** writes data to a comma separated value file.

```
1057
1058 %Start MATLAB script
1059
1060 function [] = MPM_output(tvec,lmat,Xmat)
1061
1062 % Retrieves number of components
1063 nCmps = MPM_data.cmpList();
1064 nTims = length(tvec);
1065 [~,cmpNames] = enumeration('MPM_data');
1066
1067 % Unique file ID and file name
1068 numsec = int64(now()*24*60)-2010*365.25*24*60;
1069 outfilename = strcat('MPM_run_', num2str(numsec),'.csv');
1070
1071 % Write date information
1072 ofid = fopen(outfilename, 'a');
1073 fprintf(ofid,[datestr(now()),'\n\n']);
1074 fclose(ofid);
1075
1076 % Write simulation times
1077 ofid = fopen(outfilename, 'a');
1078 fprintf(ofid,'Time (s),');
1079 fclose(ofid);
1080 dlmwrite(outfilename, tvec, '-append');
1081
1082 % Write species concentrations
1083 for k1 = 1:nCmps
1084     ofid = fopen(outfilename, 'a');
1085     fprintf(ofid,['\n','x (m)',',',',',cmpNames{k1},' (mol/m^3),']);
1086     fprintf(ofid,'\n');
1087     fclose(ofid);
1088     dlmwrite(outfilename, [lmat',Xmat(:, :, k1)'], '-append');
1089 end
1090
1091 % Write Diffusivities
1092 ofid = fopen(outfilename, 'a');
1093 fprintf(ofid,'\n');
1094 fprintf(ofid,'Diffusivities (m^2/s)\n');
1095 for k1 = 1:nCmps
1096     fprintf(ofid,[cmpNames{k1},',',',']);
1097     for k2 = 1:nTims
1098         eDif = MPM_data.valD(MPM_data.temp(tvec(k2)));
1099         fprintf(ofid,[num2str(eDif(k1)),',',',']);
1100     end
1101     fprintf(ofid,'\n');
1102 end
1103 fclose(ofid);
1104
1105 % Write Saturation Concentrations
1106 ofid = fopen(outfilename, 'a');
1107 fprintf(ofid,'\n');
1108 fprintf(ofid,'Saturation (mol/m^3)\n');
1109 for k1 = 1:nCmps
1110     fprintf(ofid,[cmpNames{k1},',',',']);
```

```
1111     for k2 = 1:nTims
1112         tempK = MPM_data.temp(tvec(k2));
1113         eCs    = MPM_data.satVals(tempK,shiftdim(Xmat(k2, :, :)))');
1114         fprintf(ofid,[num2str(eCs(k1,end))','']);
1115     end
1116     fprintf(ofid,'\n');
1117 end
1118 fclose(ofid);
1119
1120 % Write temperature information
1121 ofid = fopen(outfilename, 'a');
1122 fprintf(ofid,'\n');
1123 fprintf(ofid,'Other Time Series Data\n');
1124 fprintf(ofid,['Temp (K)','','']);
1125 for k1 = 1:nTims
1126     fprintf(ofid,[num2str(MPM_data.temp(tvec(k1))),','']);
1127 end
1128 fprintf(ofid,'\n');
1129 fclose(ofid);
1130
1131 % Write radiolysis information
1132 ofid = fopen(outfilename, 'a');
1133 fprintf(ofid,['Rad (Gy)','','']);
1134 for k1 = 1:nTims
1135     [~,dR] = MPM_data.alphRad(tvec(k1),shiftdim(Xmat(k1, :, :)))');
1136     fprintf(ofid,[num2str(dR),'','']);
1137 end
1138 fprintf(ofid,'\n');
1139 fclose(ofid);
1140
1141 % Write corrosion layer thickness information
1142 ofid = fopen(outfilename, 'a');
1143 fprintf(ofid,['Corrosion 1 (m)','','']);
1144 for k1 = 1:nTims
1145     [corr0,~] = MPM_data.regID(shiftdim(Xmat(k1, :, :)))');
1146     fprintf(ofid,[num2str(corr0),'','']);
1147 end
1148 fprintf(ofid,'\n');
1149 fprintf(ofid,['Corrosion 2 (m)','','']);
1150 for k1 = 1:nTims
1151     [~,corrL] = MPM_data.regID(shiftdim(Xmat(k1, :, :)))');
1152     fprintf(ofid,[num2str(corrL),'','']);
1153 end
1154 fprintf(ofid,'\n');
1155 fclose(ofid);
1156
1157 % Write corrosion potentials
1158 ofid = fopen(outfilename, 'a');
1159 fprintf(ofid,['Surf 1 Potential (V)','','']);
1160 for k1 = 1:nTims
1161     [~,~,~,~,eEp] = MPM_react(1,tvec(k1),shiftdim(Xmat(k1,1, :)));
1162     fprintf(ofid,[num2str(eEp),'','']);
1163 end
1164 fprintf(ofid,'\n');
1165 fprintf(ofid,['Surf 2 Potential (V)','','']);
1166 for k1 = 1:nTims
```

```
1167     [~,~,~,~,eEp] = MPM_react(2,tvec(k1),shiftdim(Xmat(k1,end,:)));
1168     fprintf(ofid,[num2str(eEp),' ','']);
1169     end
1170     fprintf(ofid,'\n');
1171     fclose(ofid);
1172
1173     % Write region densities
1174     ofid = fopen(outfilename, 'a');
1175     fprintf(ofid,'\n');
1176     eRho = MPM_data.dens();
1177     fprintf(ofid,'Density (kg/m^3)\n');
1178     fprintf(ofid,['Layer 1',' ',' ',num2str(eRho(1)),'\n']);
1179     fprintf(ofid,['Bulk   ',' ',' ',num2str(eRho(2)),'\n']);
1180     fprintf(ofid,['Layer 2',' ',' ',num2str(eRho(3)),'\n']);
1181     fclose(ofid);
1182
1183     % Write region porosities
1184     ofid = fopen(outfilename, 'a');
1185     fprintf(ofid,'\n');
1186     ePor = MPM_data.poro();
1187     fprintf(ofid,'Porosities\n');
1188     fprintf(ofid,['Layer 1',' ',' ',num2str(ePor(1)),'\n']);
1189     fprintf(ofid,['Bulk   ',' ',' ',num2str(ePor(2)),'\n']);
1190     fprintf(ofid,['Layer 2',' ',' ',num2str(ePor(3)),'\n']);
1191     fclose(ofid);
1192
1193     % Write region tortuosities
1194     ofid = fopen(outfilename, 'a');
1195     fprintf(ofid,'\n');
1196     eTor = MPM_data.tort();
1197     fprintf(ofid,'Tortuosities\n');
1198     fprintf(ofid,['Layer 1',' ',' ',num2str(eTor(1)),'\n']);
1199     fprintf(ofid,['Bulk   ',' ',' ',num2str(eTor(2)),'\n']);
1200     fprintf(ofid,['Layer 2',' ',' ',num2str(eTor(3)),'\n']);
1201     fclose(ofid);
1202
1203     return
```